

Name: _____

Date: _____

Learning Goal 1.1

Given a polynomial expression, identify the GCF and use it to find factored form.

When finding factored form of an expression, the question is **really asking** for you to find the GCF.

1. Numbers - the factors that the numbers have in common
 2. Variable(s) - counting.
- greatest common factor

Consider $8x + 4$. Using the appropriate algebra tiles:

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Arrange the tiles into rectangles (there's more than one possibility). Draw the rectangles here. Please leave lots of space between your drawings.

$$8x + 4 = \underline{4}(2x + 1)$$

$$\text{GCF}(8, 4) = \underline{4}$$

$$= 2(4x + 2) = 2 \times 2(2x + 1)$$

$$= 4(2x + 1)$$

Use algebra tiles to help you find different factored forms of the following expressions. Write down the factored expression next to each diagram.

a. $4x + 12$

$$\text{GCF}(4x, 12) = 4$$

$$4 = 2^2$$

$$12 = 2^2 \times 3$$

$$4x + 12 = 4(x + 3)$$

b. $6m + 9$

$$\text{GCF}(6m, 9) = 3$$

$$= 3(2m + 3)$$

c. $6c + 4c^2$

$$\text{GCF}(6c, 4c^2) = 2c$$

$$= 2c(3 + 2c)$$

Algebra tiles are a useful model to get started with – but not sustainable.

- positive / negative is inconsistent
- take a long time to use.
- only good for up to quadratics.

So, to factor a polynomial (or any expression for that matter):

1. Find the GCF of both numbers & variables
2. Divide the GCF out of the expression
3. Write it as a product.

Example

a. $8q^3p^5 - 12q^2p^{10}$

$$\begin{aligned} \text{GCF}(8q^3p^5, -12q^2p^{10}) \\ = 4q^2p^5 \\ = 4q^2p^5(2q - 3p^5) \end{aligned}$$

b. $12ab^2c^3 - 16a^3b^2c + 24a^4b^4c^4$

$$\begin{aligned} \text{GCF}(12ab^2c^3, -16a^3b^2c, 24a^4b^4c^4) \\ = 4ab^2c \\ = 4ab^2c(3c^2 - 4a^2 + 6a^3b^2c^3) \end{aligned}$$

c. $-18w^4x^5yz^2 - 54xy^9z^6 - 72w^{12}x^9y^3 - 7w^2x^8z$

$$\begin{aligned} \text{GCF}(-18w^4x^5yz^2, -54xy^9z^6, -72w^{12}x^9y^3, -7w^2x^8z) \\ = -x \end{aligned}$$

$$= -x(18w^4x^4yz^2 + 54y^9z^6 + 72w^{12}x^8y^3 + 7w^2x^7z)$$