

Name: \_\_\_\_\_

Date: \_\_\_\_\_

<b>Learning Goal 3.1</b>	Using all basic derivative rules.
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**Derivative**  
 the slope of the tangent at any point on  $y=f(x)$

**Derivative Function** a GRAPH of the value of the tangent at any point

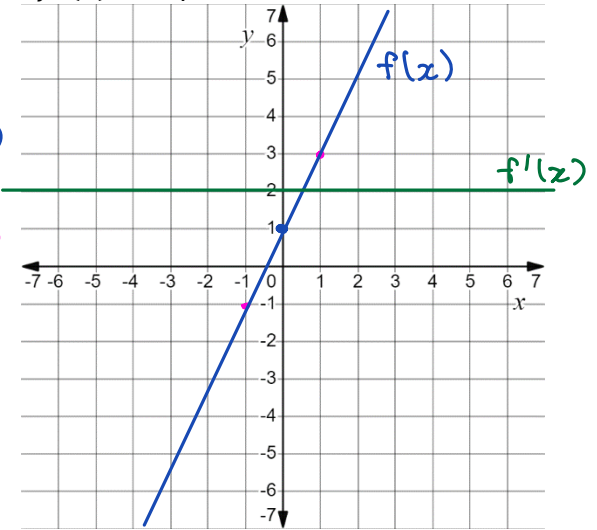
$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = f'(x)$$

GRAPHICALLY  
 \* - +/- slope  
 - inc / dec slope  
 \* - slope = 0

**Example** Given the function  $f(x) = 2x + 1$ , determine the equation of  $f'(x)$ . Graph both functions.

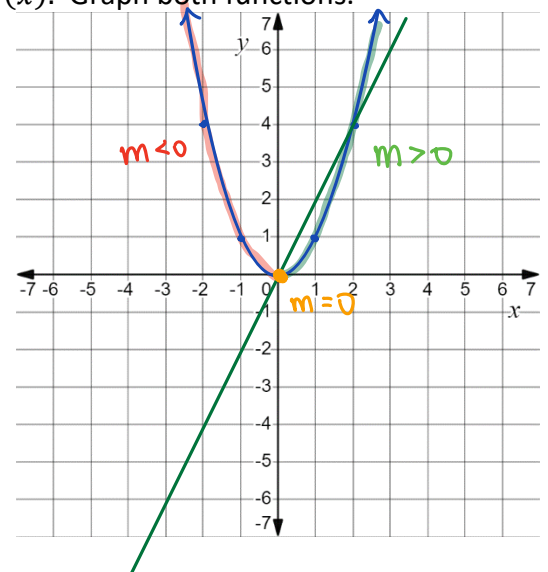
$\uparrow m = \frac{2}{1}$

$$\begin{aligned} f'(x) &= \lim_{h \rightarrow 0} \frac{2(x+h) + 1 - (2x+1)}{h} \\ &= \lim_{h \rightarrow 0} \frac{2x + 2h + 1 - 2x - 1}{h} \\ &= \lim_{h \rightarrow 0} \frac{2h}{h} \\ &= 2 \end{aligned}$$



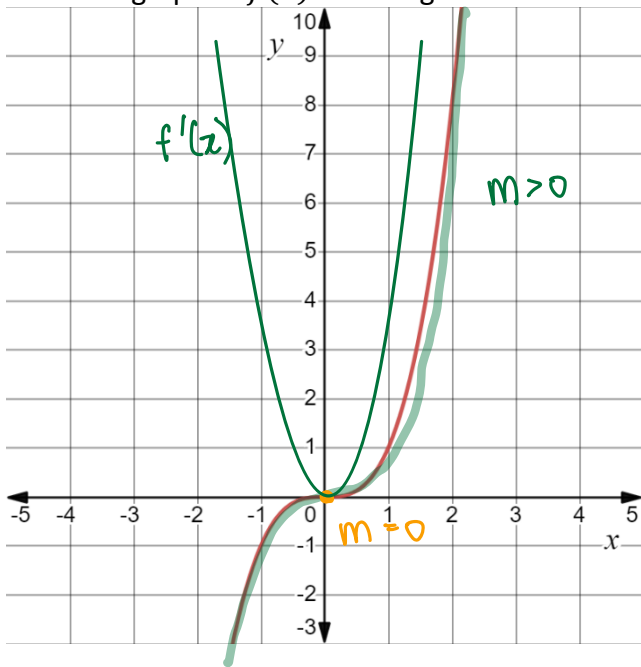
**Example** Given the function  $f(x) = x^2$ , determine the equation of  $f'(x)$ . Graph both functions.

$$\begin{aligned} f'(x) &= \lim_{h \rightarrow 0} \frac{(x+h)^2 - x^2}{h} \\ &= \lim_{h \rightarrow 0} \frac{x^2 + 2xh + h^2 - x^2}{h} \\ &= \lim_{h \rightarrow 0} \frac{h(2x+h)}{h} \\ &= 2x \end{aligned}$$

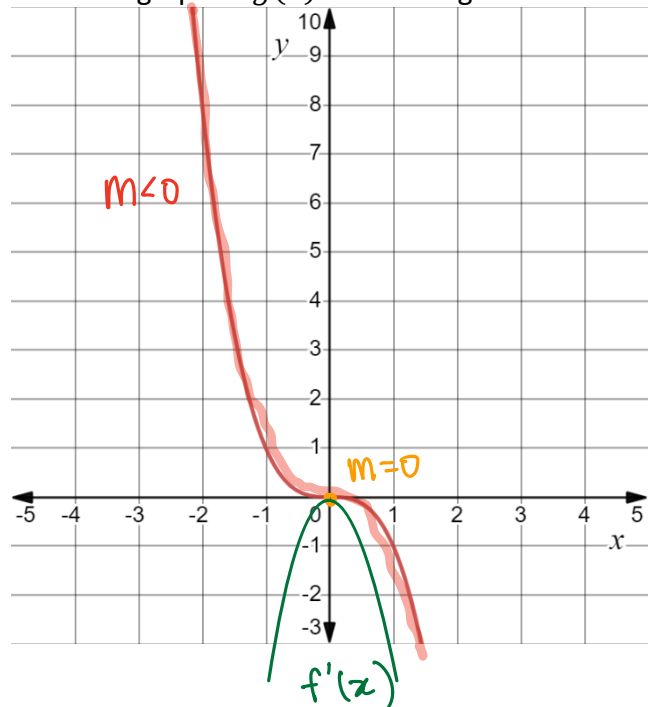


**Example** Sketch the graph of  $f'(x)$  when

a. The graph of  $f(x) = x^3$  is given.



b. The graph of  $g(x) = -x^3$  is given.



**Example** Below is the sketch of a function  $y = f(x)$ . Sketch the graph of its derivative  $y = f'(x)$ .

