

Name: _____

Date: _____

Learning Goal 3.1

Graphing and the characteristics of a graph (e.g. degree, extrema, zeros, end-behaviour).

Terminology

| Degree | Leading Coefficient | Constant |
|--------|---------------------|----------|
| | | |

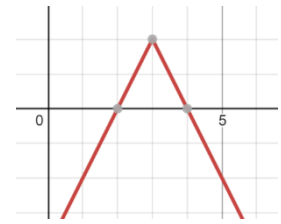
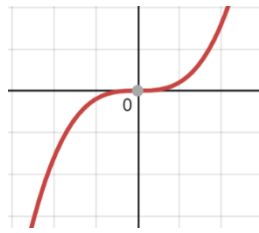
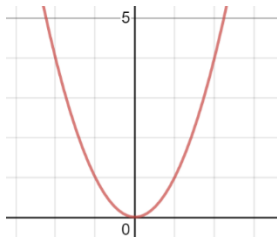
Example A polynomial function is a function that can be written in the form

$$f(x) = a_n x^n + a_{n-1} x^{n-1} + a_{n-2} x^{n-2} + \dots + a_2 x^2 + a_1 x + a_0,$$

where n is a whole number, x is a variable, the coefficients a_n to a_0 are real numbers. Which of the following functions are polynomials? For those that are polynomial functions, state the **degree**, the **leading coefficient**, and the **constant term**.

| Function | Type of Function | Degree | Leading Coefficient | Constant term |
|--|------------------|--------|---------------------|---------------|
| a. $g(x) = \sqrt{x} + 5$ | | | | |
| b. $h(x) = 2x^3 - 4x + \sqrt{8}$ | | | | |
| c. $f(x) = 3x^4$ | | | | |
| d. $k(x) = 3^x + 11$ | | | | |
| e. $f(x) = x - 7$ | | | | |
| f. $y = -0.2$ | | | | |
| g. $g(x) = 5 + 4x + \frac{1}{x}$ | | | | |
| h. $y = 2x^3 + 3x^2 - 4x - 1$ | | | | |
| i. $f(x) = \frac{2}{3}x^4 - 5x^3 - 12x + 0.56$ | | | | |
| j. $y = 3x^{-2} + 4x^2 - 6$ | | | | |

End behaviour or $\lim_{x \rightarrow \pm\infty} f(x)$



Example Use DESMOS to graph each of the following polynomial functions and complete the table:

| | $g(x) = -x^4 + 10x^2 + 5x - 4$ | $f(x) = x^3 + x^2 - 5x + 3$ |
|-------------------------------|--------------------------------|-----------------------------|
| Polynomial Type | | |
| End Behaviour | | |
| Domain | | |
| Range | | |
| Number of x – intercepts | | |
| y – intercept | | |
| Maximum and/or Minimum Values | | |

Example The x – intercepts of the graph of a function are the **zeros of the function**. We can find the zeros the function by graphing the function and determining the x – intercepts. Approximate the zeros of the function $f(x) = x^4 - 15x^2 + 20$ (to nearest tenth).