

Name: _____

Date: _____

Learning Goal 3.1

I can identify, compare, and order rational numbers.

Natural Numbers () \mathbb{N}

Counting numbers - start at 1, 2, 3, ...
 - ∞
 - no decimals or fractions.

Whole Numbers () \mathbb{W}

counting numbers + 0
 0, 1, 2, 3, ... to infinity
 - still no decimals or fractions

Positive Numbers

bigger & than the others. { \Leftrightarrow natural numbers
 ↑ the same as. - also includes decimals and fractions.
Negative Numbers
 - not positive
 - not zero

Integers () \mathbb{Z} \mathbb{Z}

- all positive and negative whole numbers
 - no fractions
 - no decimals

Rational Numbers ()

Any number that can be written as a fraction.

ex $\frac{6}{1}$ $0.735 = \frac{735}{1000}$ $0.\overline{3} = \frac{1}{3}$

- Proper Fractions

numerator is smaller than the denominator
top bottom.

$$\frac{4}{6} \div \frac{2}{2} = \frac{2}{3}$$

- Improper Fractions

numerator is bigger than the denominator.

$$\frac{6}{4} \div \frac{2}{2} = \frac{3}{2}$$

- Mixed Numbers

a whole number and a proper fraction

$$1\frac{2}{4} \div \frac{2}{2} = 1\frac{1}{2}$$

Examples of Rational Numbers ():

- 2 can be expressed in the form $\frac{a}{b}$ as $\frac{2}{1} = \frac{4}{2} = \frac{8}{4} = \frac{100}{50}$

- $-\frac{13}{9} =$ not reducible $= 1.\overline{4}$

- $\frac{\sqrt{16}}{3} = \frac{4}{3} \therefore 1\frac{1}{3}$

$$\sqrt{16} = \sqrt{4 \times 4} = 4$$

- $\sqrt{4} = 2$ or $2\frac{1}{2} =$ or $\frac{1}{4} =$ \therefore since all all are

$0.\overline{6} = \frac{2}{3} = 0.66666 \dots \therefore$ repeating decimal (repeats) } rational.
 $0.\overline{45} = \frac{5}{11} = 0.454545 \dots \therefore$ " (repeats)

All decimals that repeat or terminate (stop) are rational.

$$\frac{4}{3} = 1\frac{1}{3} = \frac{3+1}{3} = \frac{3}{3} + \frac{1}{3} = 1 + \frac{1}{3}$$

$$0.455555 \dots \neq 0.\overline{45} = 0.4\overline{5}$$

Irrational Numbers

- any number that is not a rational number
- cannot be written as a fraction.
- non-repeating, non-terminating decimals.

Examples of irrational numbers:

- $\sqrt{2} = 1.41421356 \dots \therefore$ Irrational (never terminate or repeats)
- $\pi = 3.14159265 \dots \therefore$ Irrational (never " or ")
- $1.23223222322223222223 \dots$ Even though it has a pattern, it does not repeat or terminate and therefore it is irrational

Real Numbers () \mathbb{R}

- all the sets combined

