

Name: \_\_\_\_\_

Date: \_\_\_\_\_

<b>Learning Goal 4.1</b>	Identify and order irrational numbers.
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A square root represents:

the side length of a given area.

$$\text{side length} = \sqrt{\text{area}} \text{ for a square.}$$

Many square roots result in irrational numbers, but we should not be too quick to judge! Especially without a calculator ...

**Example** Consider the relationship between the following 4 numbers:

$$400 = 4 \times 100 \quad 40 = 4 \times 10 \quad \sqrt{4} = 2 \quad 0.4 = \frac{4}{10} \quad 0.04 = \frac{4}{100}$$

$$\sqrt{400} = 20 \quad \sqrt{4} = 2 \quad \sqrt{0.04} = 0.2$$

How many of these numbers have **rational square roots**? How many have **irrational square roots**? Why?

$$400 = 2^4 \times 5^2$$

$$\sqrt{2^4 \times 5^2} = 2^2 \times 5$$

$$\frac{4}{100} = \frac{2^2}{2^2 \times 5^2} = \frac{1}{5^2}$$

$$\sqrt{\frac{1}{5^2}} = \frac{1}{5}$$

**Example** Try again!

90      9      0.9      0.09      0.009      0.0009

How many of these numbers have **rational square roots**? How many have **irrational square roots**? Why?

$$\sqrt{9} = 3$$

$$\sqrt{0.09} = 0.3$$

$$\sqrt{0.0009} = 0.03$$

$$\sqrt{0.0009} = \sqrt{\frac{9}{10000}} = \sqrt{\frac{3^2}{10^4}} = \frac{3}{10^2} = 0.03$$

Invert!

**Example** For each number below, write an equivalent form as the table specifies.

	As a square root	As a cube root	As a fourth root
$5 =$	$\sqrt{25}$	$\sqrt[3]{125} = \sqrt[3]{5^3}$	$\sqrt[4]{5^4} = \sqrt[4]{625}$
$\frac{5}{10} = 0.5 =$	$\sqrt{\frac{5^2}{10^2}} = \sqrt{\frac{25}{100}} = \sqrt{0.25}$	$\sqrt[3]{\frac{5^3}{10^3}} = \sqrt[3]{\frac{125}{1000}} = \sqrt[3]{0.125}$	$\sqrt[4]{\frac{5^4}{10^4}} = \sqrt[4]{\frac{625}{10000}} = \sqrt[4]{0.0625}$
$5 \times 10 = 50 =$	$\sqrt{5^2 \times 10^2} = \sqrt{2500}$		

Consider the numbers that have been given to you within your table group


1. Decide who among you has an irrational number
2. Place your 4 numbers in order from **smallest to biggest** on the number line below

