

Name: _____

Date: _____

| | |
|--------------------------|---|
| Learning Goal 4.1 | Given a quadratic equation, identify the number of solutions, zeros, roots or x – intercepts. |
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Equations vs. Functions

Solve.

- you control input
- function gives the output

Recall Graphing Quadratic Functions

- Vertex Form
- Standard Form
- Factored Form

$$y = a(x-p)^2 + q$$

$$y = ax^2 + bx + c$$

$$y = (x-m)(x-n)$$

← what are the x -intercepts?

Example Determine the roots of the quadratic equation $x^2 - 6x + 9 = 0$ by graphing.

$$\begin{aligned} -3 \times -3 &= 9 \\ -3 + -3 &= -6 \end{aligned}$$

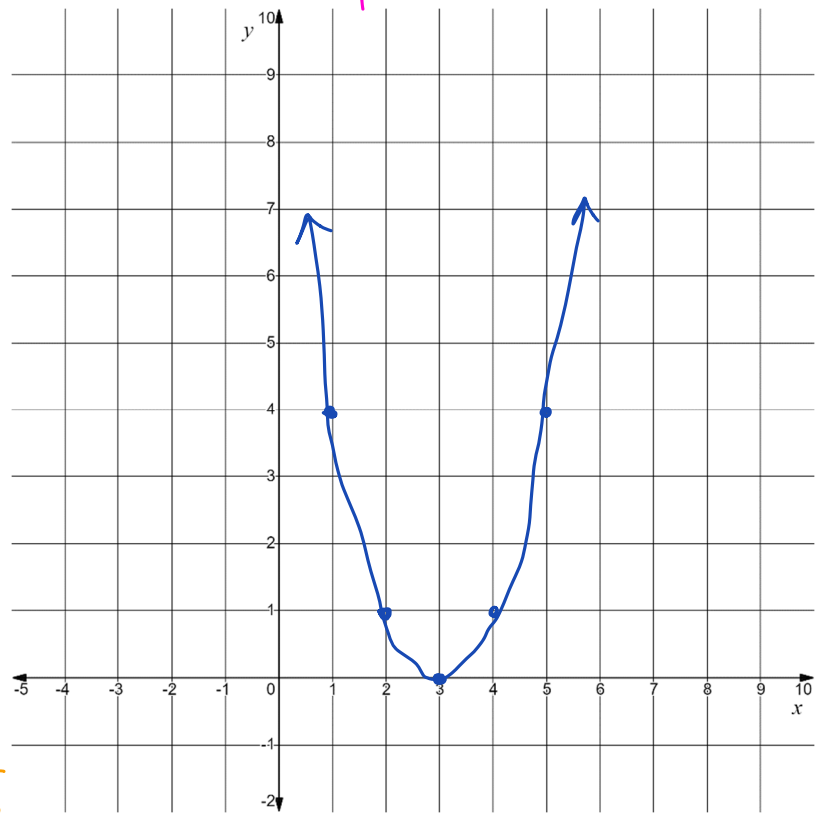
$$\begin{aligned} (x-3)(x-3) &= 0 \\ (x-3)^2 &= 0 \\ x-3 &= 0 \\ x &= 3 \end{aligned}$$

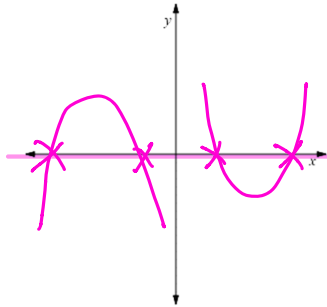
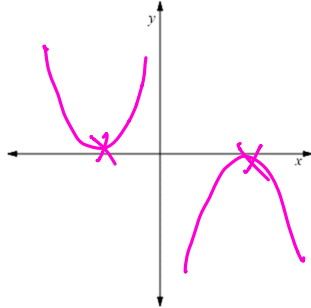
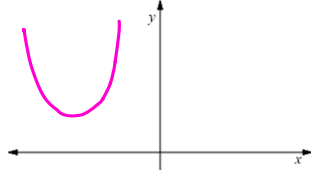
Example Solve $3m^2 + 6m = -6$ by graphing.

$$\begin{aligned} 3m^2 + 6m + 6 &= 0 \\ 3(m^2 + 2m + 2) &= 0 \end{aligned}$$

Not factorable
 $_ \times _ = 2$
 $_ + _ = 2$

↳ find another method!



| 😊 or 😞 | Vertex | Number of x – intercepts or solutions |
|--------|----------------------------|--|
| 😊 | below x -axis $a < 0$ | 2 x -int.  |
| 😞 | $a > 0$ | |
| 😊 | $a = 0$ | 1 x -int.  |
| 😞 | $a = 0$ | |
| 😊 | $a > 0$ | 0 x -int.  |
| 😞 | $a < 0$ | |

← still looking for x -intercepts.

Example Determine the number of zeros of the following functions.

a. $y = -0.07(x - 3.1)^2 - 4.25$



$a < 0$

there are no zeros

b. $y = x^2 + 18x + 81$

$\frac{9}{9} \times \frac{9}{9} = 81$
 $\frac{9}{9} + \frac{9}{9} = 18$

$= (x+9)(x+9)$
 $= (x+9)^2$

there is one zero

c. $y = -x^2 + 4x - 1$

$= -(x^2 - 4x) - 1$
 $= -(x^2 - 4x + 4 - 4) - 1$
 $= -(x^2 - 4x + 4) + 4 - 1$
 $= -(x - 2)^2 + 3$

there are two zeros.