

Name: _____

Date: _____

What is a solution? - the answer
 - add water to chemicals

→ 2 equations - where they cross (graphically)
 - where the equations are equal (algebraically)

Example Is the point $(-1, 1)$ a solution to:

$$\begin{aligned} 7x + 6y &= 1 \\ x + 2y &= -3 \end{aligned}$$

Justify your answer.

$$\begin{aligned} 7(-1) + 6(1) & \\ &= -7 + 6 \\ &= -1 \neq 1 \end{aligned}$$

$$\begin{aligned} (-1) + 2(1) & \\ &= -1 + 2 \\ &= 1 \neq -3 \end{aligned}$$

* these lines do not cross through the point $(-1, 1)$

Example Find the solution to each of the following systems:

a.

* common points

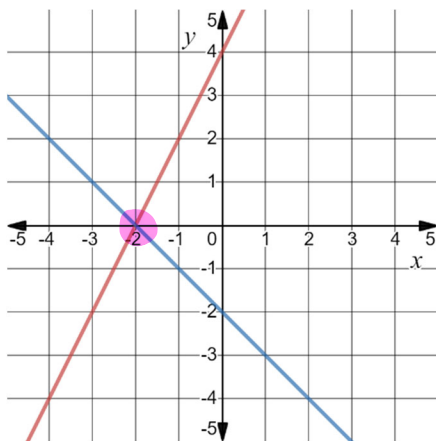
x	y
-4	0
-2	-2
0	-4
2	-6
4	-8

x	y
-2	-14
-1	-12
0	-10
1	-8
2	-6

the solution will be $(2, -6)$

b.

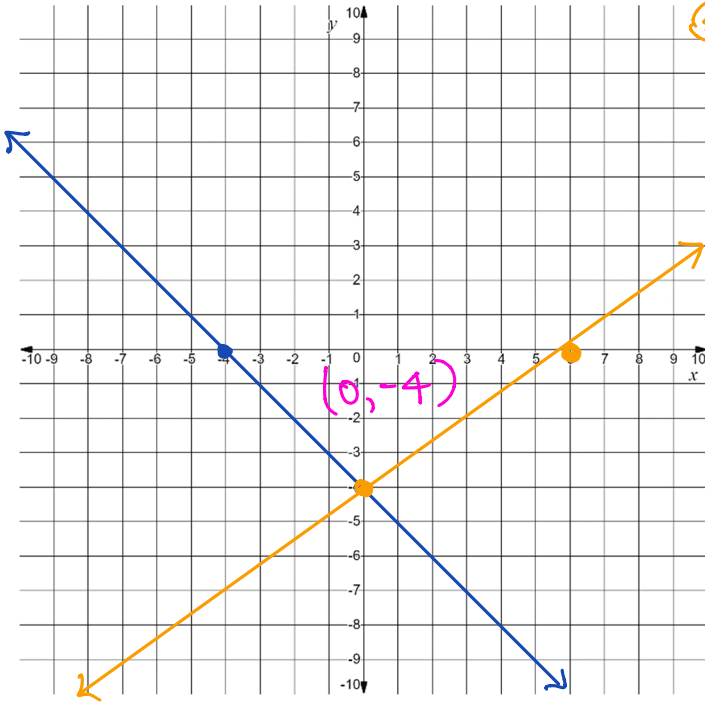
* intersection point



$(-2, 0)$

Example Solve the following system graphically. Check your solution.

① $x + y = -4$
 ② $2x - 3y = 12$



x-int
(y=0) $x + 0 = -4$
 $x = -4$

y-int
(x=0) $0 + y = -4$
 $y = -4$

x-int
(y=0) $2x - 3(0) = 12$
 $\frac{2x}{2} = \frac{12}{2}$
 $x = 6$

y-int
(x=0) $2(0) - 3y = 12$
 $\frac{-3y}{-3} = \frac{12}{-3}$
 $y = -4$

CHECK: $0 + (-4) = -4$ ✓

$2(0) - 3(-4) = 0 + 12 = 12$ ✓

Example A school raised \$140 by collecting 2000 cans and glass bottles for recycling. The school received 5¢ for a can and 10¢ for a bottle. How many cans and bottles were returned?

c = the # of cans returned
 b = the # of bottles returned.

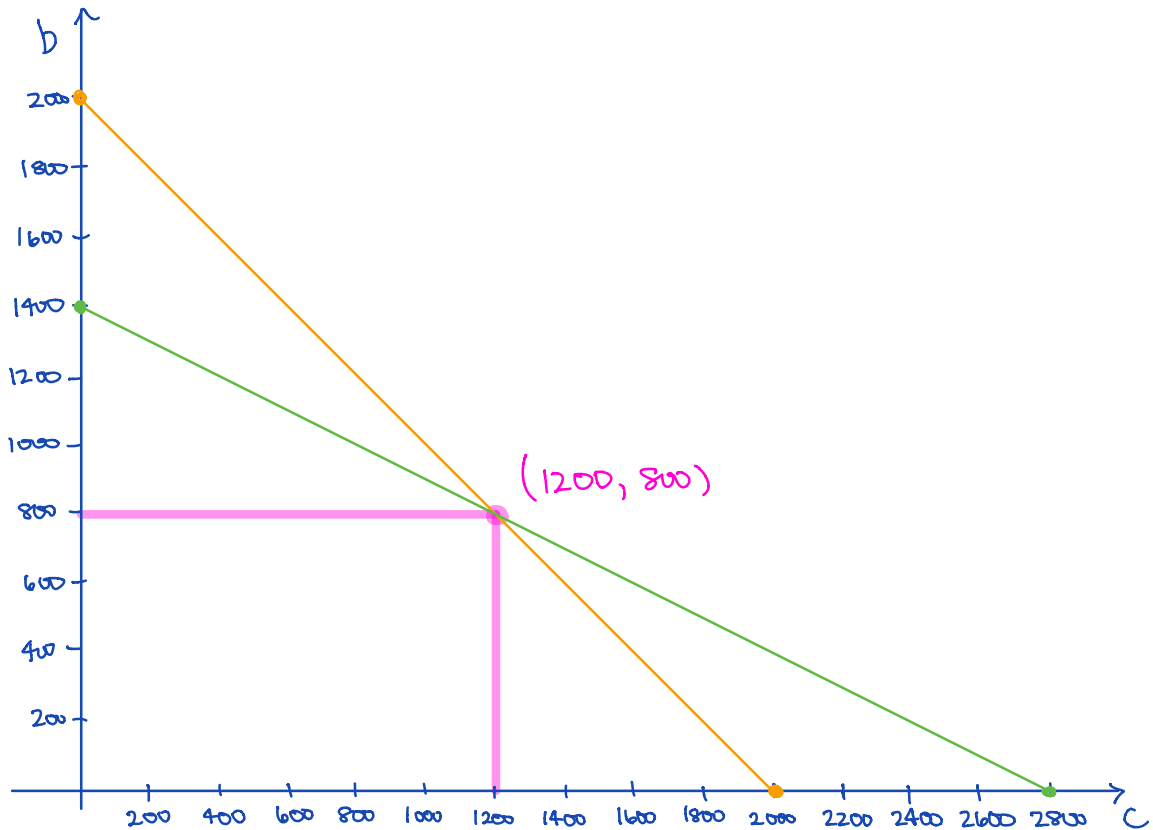
$c + b = 2000$ ①
 $5c + 10b = 14000$ ②

c-int
(b=0) $c + 0 = 2000$
 $c = 2000$

b-int
(c=0) $0 + b = 2000$
 $b = 2000$

c-int
(b=0) $5c + 10(0) = 14000$
 $\frac{5c}{5} = \frac{14000}{5}$
 $c = 2800$

b-int
(c=0) $5(0) + 10b = 14000$
 $\frac{10b}{10} = \frac{14000}{10}$
 $b = 1400$



$$c + b = 2000$$

$$5c + 10b = 14000$$

CHECK: $1200 + 800 = 2000$ ✓

$5(1200) + 10(800) = 6000 + 8000 = 14000$ ✓

They returned 1200 cans and 800 glass bottles.