

Name: _____

Date: _____

A quadratic relationship is one that has a degree of 2.

The standard form of a quadratic function is $y = ax^2 + bx + c$.

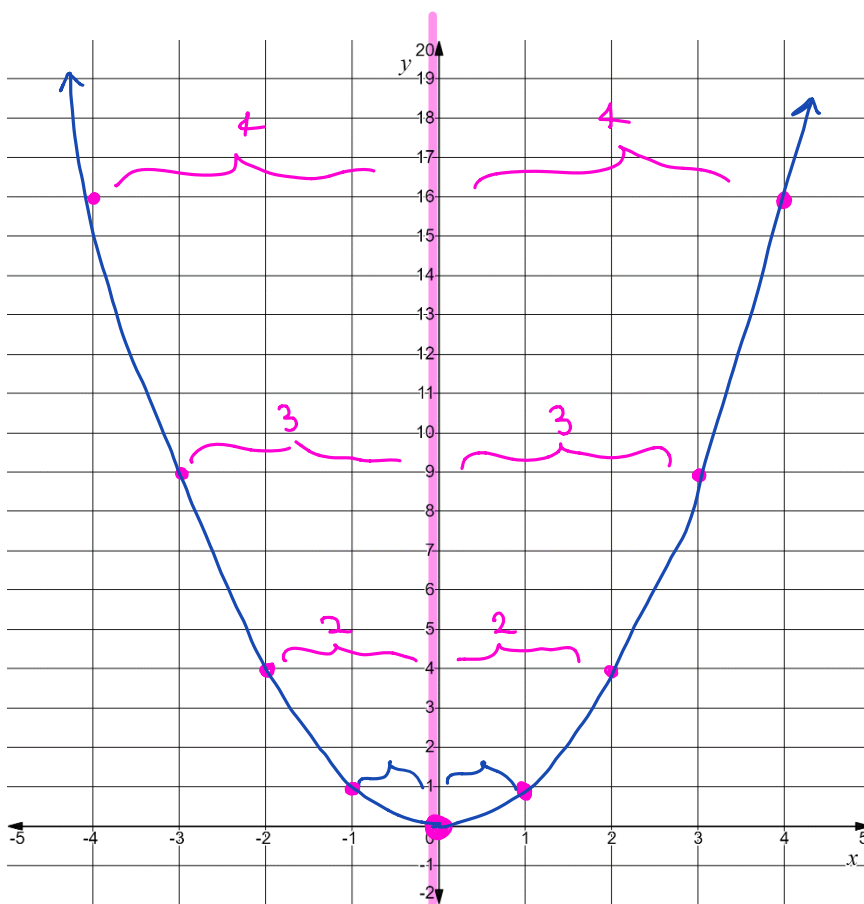
The "basic" quadratic function is $y = x^2$. Complete the table of values and then graph the function.

x	-4	-3	-2	-1	0	1	2	3	4
y	16	9	4	1	0	1	4	9	16

This shape is called a

Graph features:

- Vertex is the middle of your parabola. - your mirror point
 $(0, 0)$
- x-intercept is where you cross or touch the x-axis
horizontal
 $(0, 0)$
- y-intercept is where you cross the y-axis
vertical
 $(0, 0)$
- Axis of symmetry mirror that runs through the vertex
 $x = 0$



Example Consider $y = x^2 + 4x + 3$.

- From this form of the equation we know the

Standard form - we know the y-intercept (x=0)

$$y = (0)^2 + 4(0) + 3$$

- If we factor this equation, we will know the

$$\begin{aligned}
 \underline{3} \times \underline{1} &= 3 \\
 \underline{3} + \underline{1} &= 4 \\
 y &= \underline{x^2 + 3x} + \underline{x + 3} \\
 &= x(x+3) + (x+3) \\
 &= (x+3)(x+1)
 \end{aligned}$$

- we can find the x-intercepts (y=0)

- We can find the vertex by

by finding the distance between the x-int. and cutting it in half.

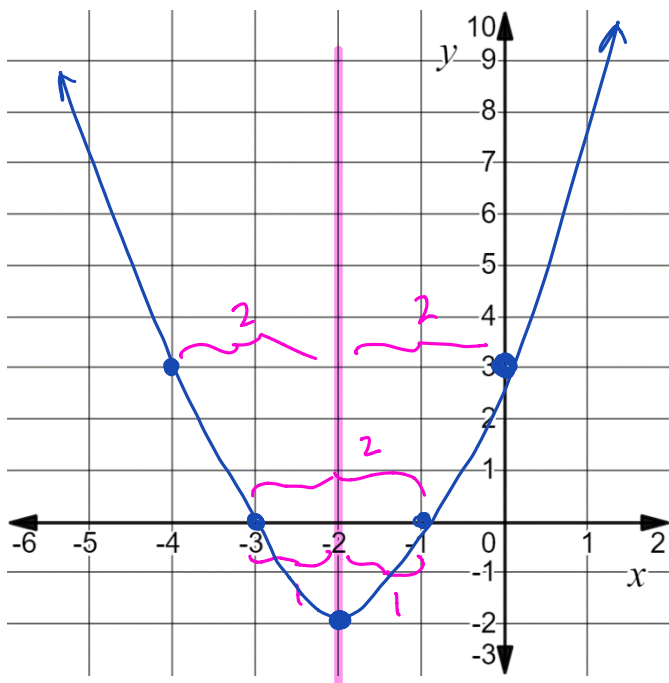
$$\begin{aligned}
 0 &= (x+3)(x+1) \\
 \downarrow & \qquad \qquad \downarrow \\
 x+3 &= 0 \quad \text{or} \quad x+1 = 0 \\
 -3 \quad -3 & \qquad \qquad -1 \quad -1 \\
 \underline{x = -3} & \qquad \qquad \underline{x = -1}
 \end{aligned}$$

- The axis of symmetry

$$x = -2$$

$$\begin{aligned}
 y &= (-2)^2 + 4(-2) + 3 \\
 &= 4 - 8 + 3 \\
 &= -4 + 3 \\
 &= -1 \qquad \text{vertex } (-2, -1)
 \end{aligned}$$

x	-5	-4	-3	-2	-1	0	1
y	7	3	0	-1	0	3	7



We are going to use <http://www.mathopenref.com/quadraticexplorer.html> to explore quadratic functions.

$$y = ax^2 + bx + c$$

- What happens as a changes?

if a is -ve - frowning
 if a is +ve - smiling

- big a value makes it tall & skinny
 - small a value makes it wide.

- What happens as b changes?

- the curve dances

- What happens as c changes?

- the y -intercept changes

- What happens if $a = 0$?

- not a parabola
 - just a line

- What happens if $b = 0$?

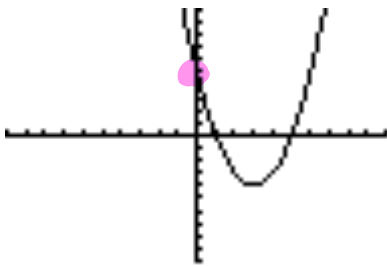
- the vertex is on the y -axis.

- What happens if $c = 0$?

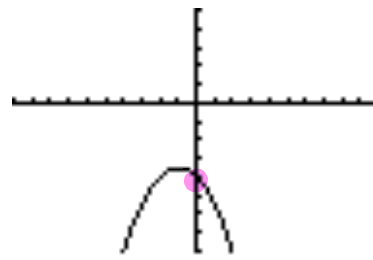
the y -intercept is zero

Example For the graphs below, predict whether a, b, c are positive, negative or zero.

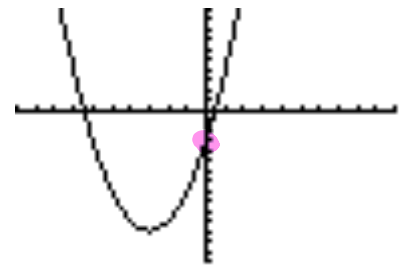
a.



b.



c.



a +ve

b +ve (vertex has +ve x value)

c +ve

-ve

-ve

-ve

+ve

-ve

-ve.