

Name: \_\_\_\_\_

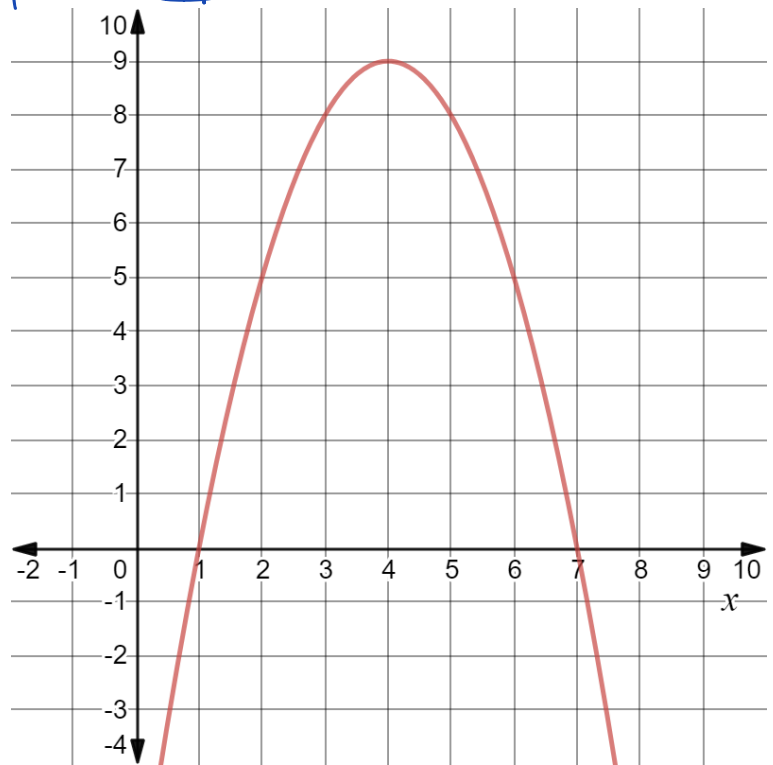
Date: \_\_\_\_\_

**Recall** A quadratic function can be written in one of three forms:

1. **standard form**  $y = ax^2 + bx + c$  ↖ y-intercept:
2. **factored form**  $y = (x - m)(x - n)$  x-intercept(s)  
x = m, n
3. **vertex form**  $y = a(x - p)^2 + q$  vertex (p, q)

**Example** On the following graph identify the following features:

$$\begin{aligned}
 & \quad \quad \quad x=1 \quad \quad \quad x=7 \\
 y &= -(x-1)(x-7) \\
 &= -(x^2 - 7x - x + 7) \\
 & \quad \quad \quad \text{F} \quad \quad \quad \text{O} \quad \quad \quad \text{I} \quad \quad \quad \text{L} \\
 &= -(x^2 - 8x + 7) \\
 &= -x^2 + 8x - 7
 \end{aligned}$$



<p>1. y-intercept we can't see it ☹️ <math>y = -7</math></p>	<p>2. x-intercept(s) <math>x = 1, 7</math></p>	<p>3. Equation of the axis of symmetry <math>x = 4</math></p>
<p>4. Coordinates of the vertex <math>(4, 9)</math></p>	<p>5. Maximum or minimum value <math>y = 9</math></p>	<p>6. Domain and range Domain: <math>x \in \mathbb{R}</math> Range: <math>y \leq 9</math></p>

Of Quadratic Functions

**Example** Consider the quadratic function  $y = x^2 - 4x + 4$ . Find the  $y$ -intercept, then factor to find the  $x$ -intercept(s). Graph the function either by using these coordinates, or by completing the table of values.

$x$	0	1	2	3	4	5	6
$y$							

$y$ -int:  $y = 4$

$y = x^2 - 4x + 4$

$-2 \times -2 = 4$

$-2 + -2 = -4$

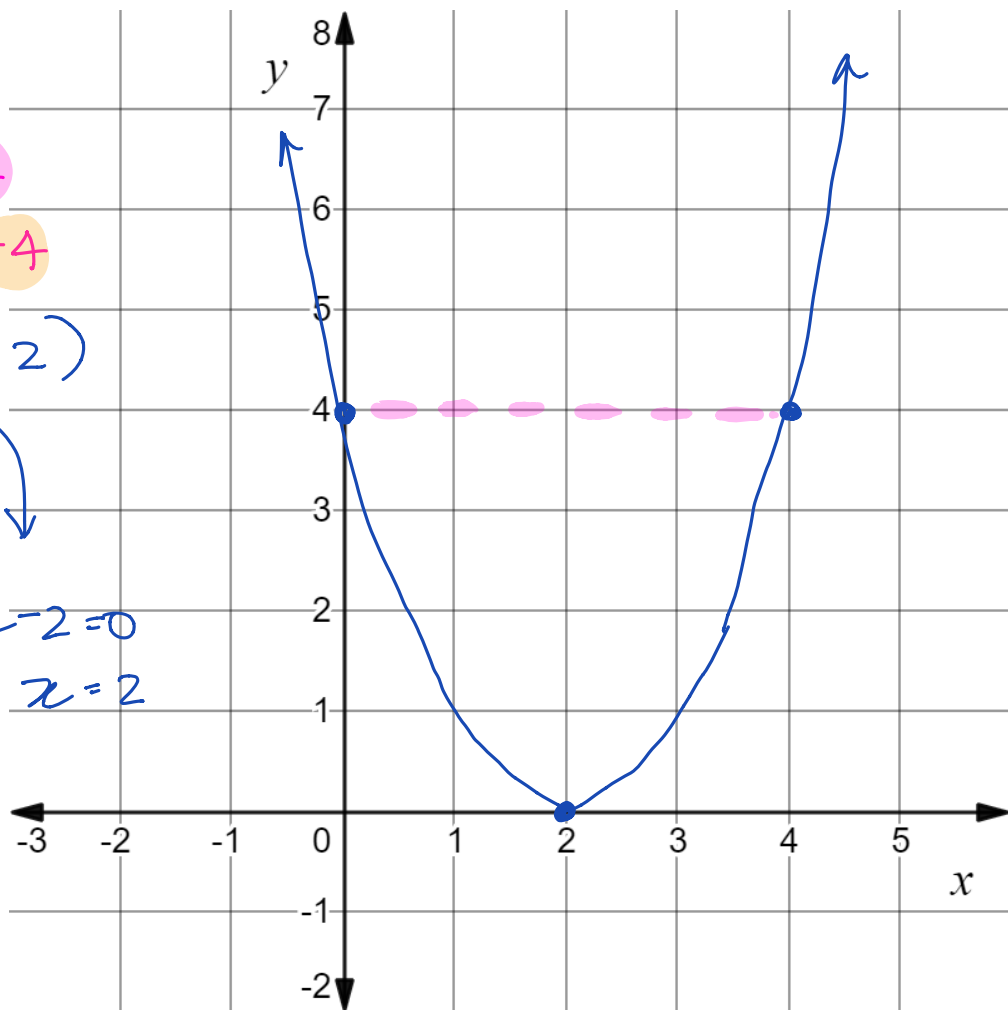
$= (x - 2)(x - 2)$

↓

$x$ -int ( $y = 0$ )

$x - 2 = 0$   
 $x = 2$

$x - 2 = 0$   
 $x = 2$



Determine the:

<p>1. <math>y</math>-intercept <math>y =</math> <math>y = 4</math> <math>(0, 4)</math></p>	<p>2. <math>x</math>-intercepts <math>x =</math> <math>x = 2</math> <math>(2, 0)</math></p>	<p>3. Equation of the axis of symmetry <math>x =</math> <math>x = 2</math></p>
<p>4. Coordinates of the vertex <math>(x, y)</math> <math>(2, 0)</math></p>	<p>5. Maximum or minimum value <math>y =</math> <math>y = 0</math></p>	<p>6. Domain and range Domain: <math>x \in \mathbb{R}</math> Range: <math>y \geq 0</math></p>

Ex. #1 Consider the quadratic function  $y = -x^2 + 7x - 10$ . Find the  $y$ -intercept, then factor to find the  $x$ -intercept(s). Graph the function either by using these coordinates, or by completing the table of values.

$x$	0	1	2	3	4	5	6
$y$							

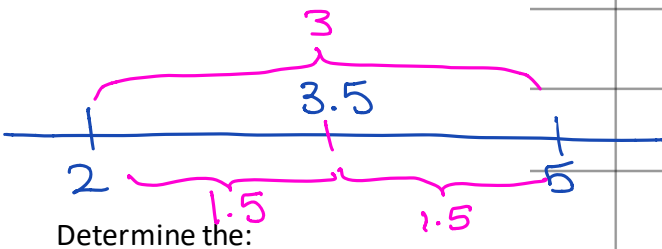
$$y = -(x^2 - 7x + 10)$$

$$\underline{-5} \quad \underline{x-2} = 10$$

$$\underline{-5} + \underline{-2} = -7$$

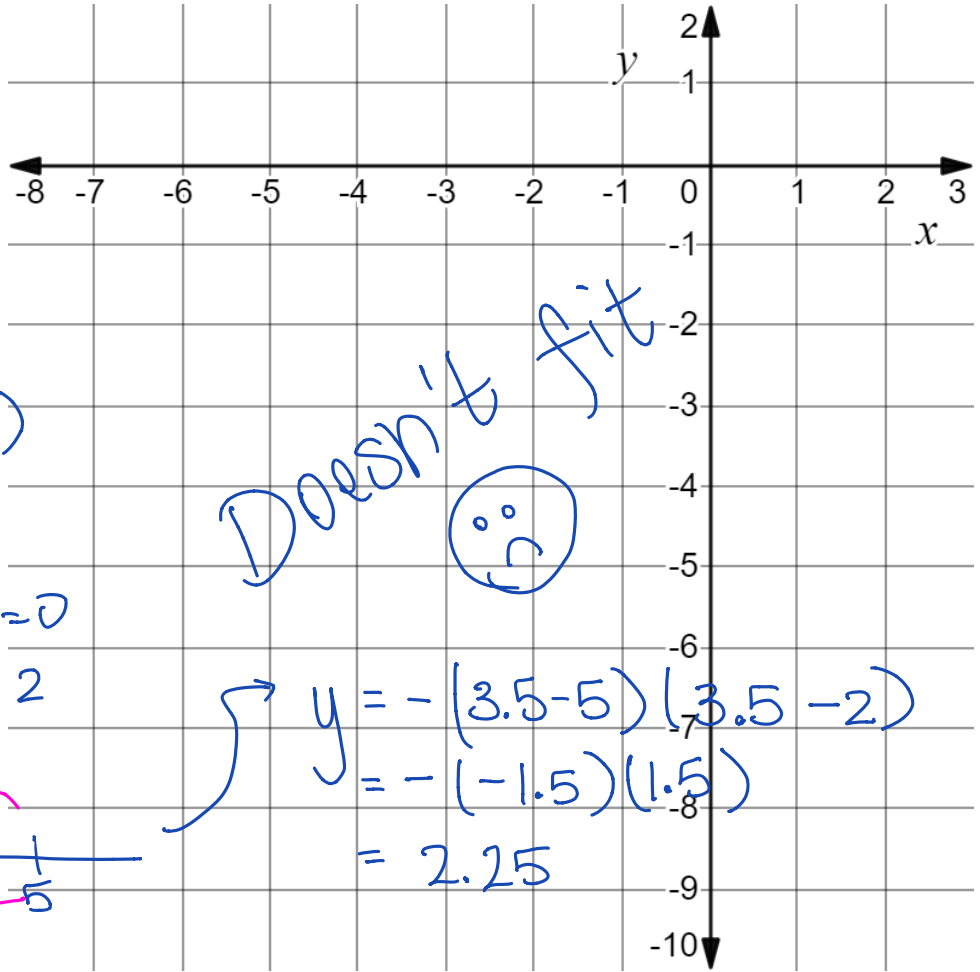
$$y = -(x-5)(x-2)$$

$$\begin{aligned} x-5 &= 0 & x-2 &= 0 \\ x &= 5 & x &= 2 \end{aligned}$$



Doesn't fit 😞

$$\begin{aligned} y &= -(3.5-5)(3.5-2) \\ &= -(-1.5)(1.5) \\ &= 2.25 \end{aligned}$$



1. $y$ -intercept $y = -10$	2. $x$ -intercepts $x = 5$ $x = 2$	3. Equation of the axis of symmetry $x = 3.5$
4. Coordinates of the vertex $(3.5, 2.25)$	5. <u>Maximum</u> or minimum value $y = 2.25$	6. Domain and range Domain: $x \in \mathbb{R}$ Range: $y \leq 2.25$