

Name: _____

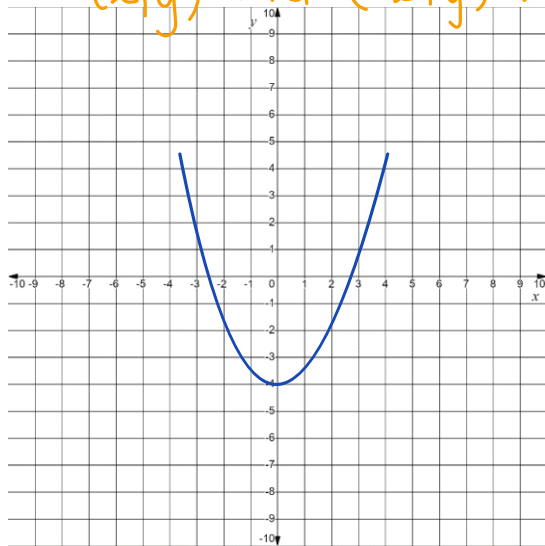
Date: _____

Learning Goal 1.1

Understanding new ideas about functions and applying that to previously knowledge.

Even Function has symmetry around the y-axis

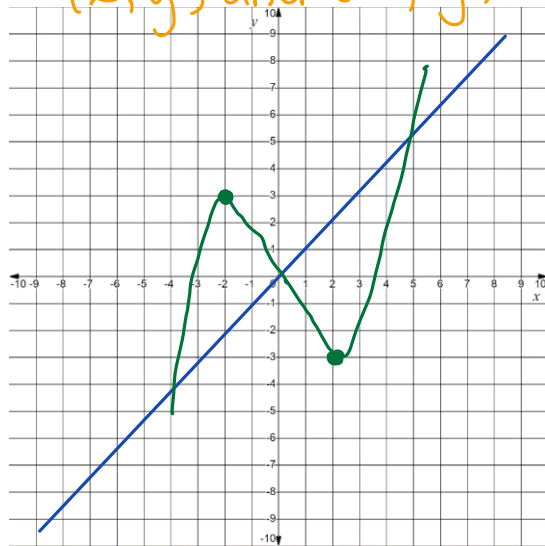
(x, y) and $(-x, y)$ to both be on the graph.



$$f(-x) = f(x)$$

Odd Function has rotational symmetry of 180°

(x, y) and $(-x, -y)$ to both be on the graph.



$$f(-x) = -f(x)$$

Example Determine whether the function is even, odd or neither.

a. $f(x) = x^5 + x$

b. $g(x) = 1 - 2x^4$

c. $h(x) = 2x - 3x^2$

$$\begin{aligned} f(-x) &= (-x)^5 + (-x) \\ &= -x^5 - x \\ &= -(x^5 + x) \end{aligned}$$

ODD!

$$\begin{aligned} g(-x) &= 1 - 2(-x)^4 \\ &= 1 - 2x^4 \\ &= g(x) \end{aligned}$$

EVEN

$$\begin{aligned} h(-x) &= 2(-x) - 3(-x)^2 \\ &= -2x - 3x^2 \\ &= -(2x + 3x^2) \end{aligned}$$

NEITHER

The Difference Quotient

$$\frac{f(x+h) - f(x)}{h}$$

↪ BASIS OF DERIVATIVES
WHEN WE LET $h \rightarrow 0$

Example Evaluate the difference quotient for the following function. Simplify your answer.

a. $f(x) = 2 - x^2$

$$\begin{aligned} f(x+h) &= 2 - (x+h)^2 \\ &= 2 - (x^2 + 2xh + h^2) \\ &= 2 - x^2 - 2xh - h^2 \end{aligned}$$

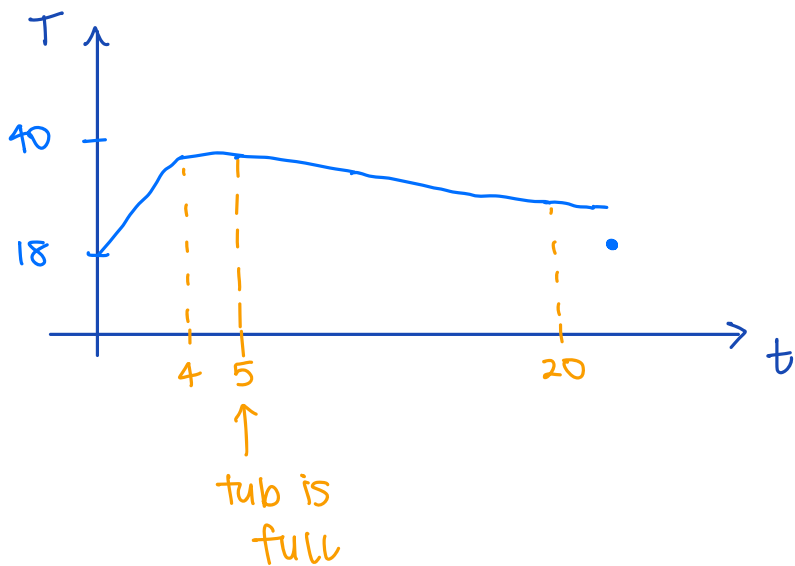
$$\begin{aligned} \frac{f(x+h) - f(x)}{h} &= \frac{[2 - x^2 - 2xh - h^2] - [2 - x^2]}{h} \\ &= \frac{-2xh - h^2}{h} \\ &= -2x - h \end{aligned}$$

b. $y = -x^2 + 4x + 1$

$$\begin{aligned} &-(x+h)^2 + 4(x+h) + 1 \\ &= -(x^2 + 2xh + h^2) + 4x + 4h + 1 \\ &= -x^2 - 2xh - h^2 + 4x + 4h + 1 \end{aligned}$$

$$\begin{aligned} &= \frac{[-x^2 - 2xh - h^2 + 4x + 4h + 1] - [-x^2 + 4x + 1]}{h} \\ &= \frac{-2xh - h^2 + 4h}{h} \\ &= -2x - h + 4 \end{aligned}$$

Example When you turn on a hot-water faucet, the temperature T of the water depends on how long the water has been running. Draw a rough graph of T as a function of the time t that has elapsed since the faucet was turned.



ASSUMPTIONS

- empty bathtub starting @ 18°C
- water is 40°C
- water runs for 5 min.