Name: $\qquad$ Date: $\qquad$

## Learning Goal 4.1 $\quad$ Using derivative tests for curve sketching.

Concavity given that $f^{\prime}(c)=0$, we have three cases





And this is how $f^{\prime}(x)$ is changing in each case





And this is how $f^{\prime \prime}(x)$ is changing in each case.




Example Discuss the concavity of $y=\sqrt{x}$ and $y=\sqrt[3]{x}$.

Concavity can replace the First Derivative Test too!
Theorem

Inflection Points are points $(c, f(c))$ where

Example Given that $y=x^{4}-4 x^{3}$, find the inflection points, the intervals over which the function is concave up or down, and use $f^{\prime \prime}(x)$ to find any local extrema.

