

Name: \_\_\_\_\_

Date: \_\_\_\_\_

**Learning Goal 4.1**

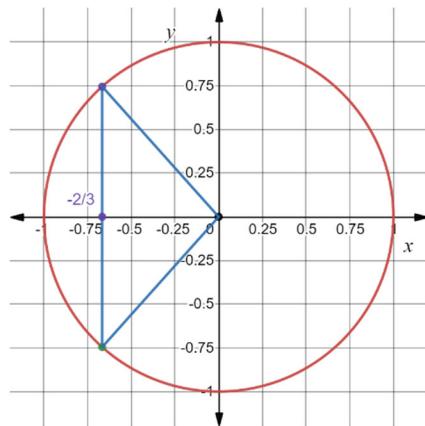
Examining angles in standard position in both radians and degrees. Exploring the unit circle, reference and coterminal angles and special angles.

**More Questions - Solutions**

1. Find the co-ordinate(s) of all points on the unit circle that satisfy the conditions below. Include a diagram in your solution.

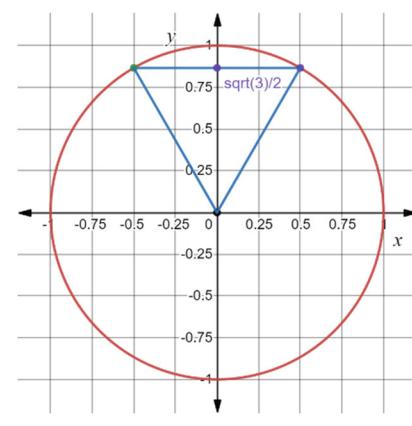
a.  $x$  – coordinate of  $-\frac{2}{3}$ .

$$\begin{aligned}x^2 + y^2 &= 1 \\ \left(\frac{2}{3}\right)^2 + y^2 &= 1 \\ \frac{4}{9} + y^2 &= 1 \\ y^2 &= \frac{5}{9} \\ y &= \pm \frac{\sqrt{5}}{3}\end{aligned}$$

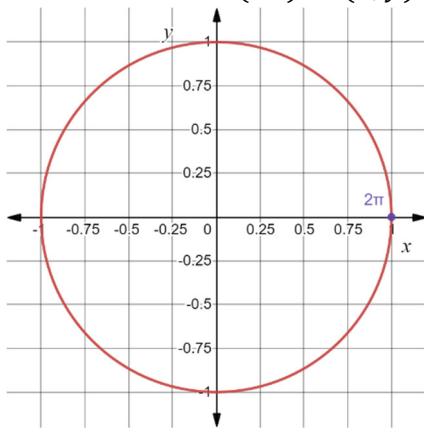


b.  $y$  – coordinate of  $\frac{\sqrt{3}}{2}$ .

$$\begin{aligned}x^2 + y^2 &= 1 \\ x^2 + \left(\frac{\sqrt{3}}{2}\right)^2 &= 1 \\ x^2 + \frac{3}{4} &= 1 \\ x^2 &= \frac{1}{4} \\ x &= \pm \frac{1}{2}\end{aligned}$$

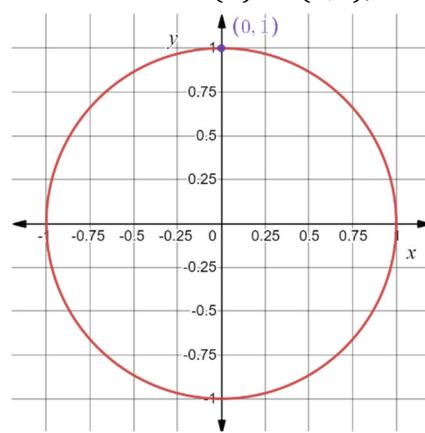


2. Evaluate  $P(2\pi) = (x, y)$ .



$$P(2\pi) = (1, 0)$$

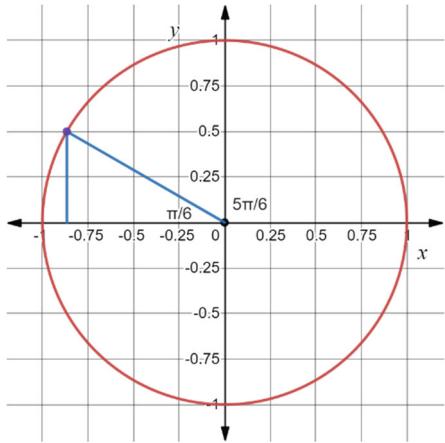
3. Given  $P(\theta) = (0,1)$ , find  $\theta$  in radians.



$$P\left(\frac{\pi}{2}\right) = (0, 1)$$

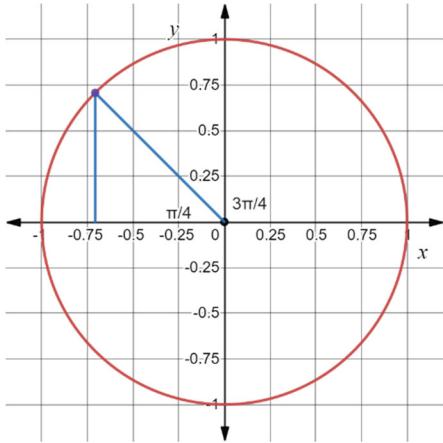
4. Evaluate.

a.  $P\left(\frac{5\pi}{6}\right)$



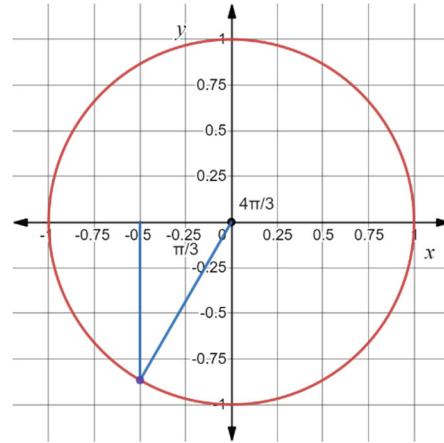
$$P\left(\frac{5\pi}{6}\right) = \left(-\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$$

b.  $P\left(\frac{3\pi}{4}\right)$



$$P\left(\frac{3\pi}{4}\right) = \left(-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$$

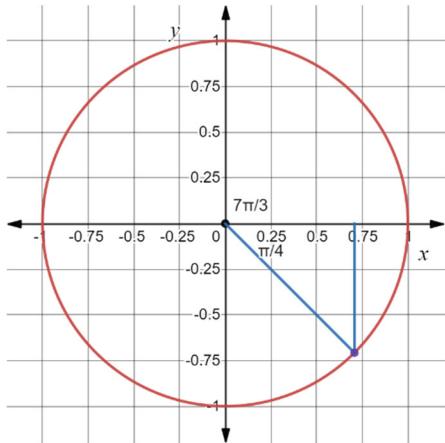
c.  $P\left(\frac{4\pi}{3}\right)$



$$P\left(\frac{4\pi}{3}\right) = \left(-\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$$

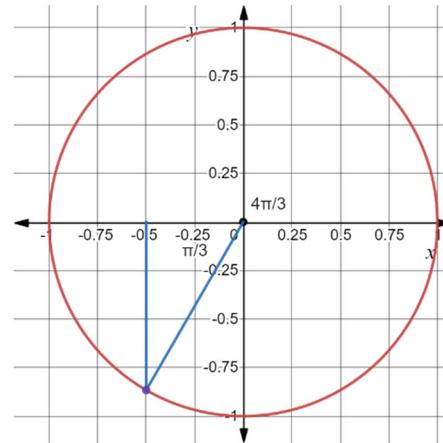
5. Identify the measure for the central angle  $\theta$  in the interval  $0 \leq \theta \leq 2\pi$  such that  $P(\theta)$  is the given point.

a.  $\left(\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$



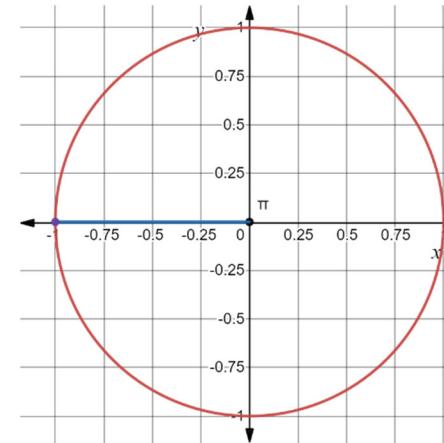
$$P\left(\frac{7\pi}{6}\right) = \left(\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$$

b.  $\left(-\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$



$$P\left(\frac{4\pi}{3}\right) = \left(-\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$$

c.  $(-1, 0)$



$$P(\pi) = (-1, 0)$$