

Name: _____

Date: _____

Learning Goal 6.1

Using identities to reduce complexity in expressions and solve equations.

More Questions**Sum and Difference Identities**

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$\sin(A + B) = \sin A \cos B + \cos A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

1. Verify the identity
- $\sin(A + B) = \sin A \cos B + \cos A \sin B$
- numerically, without a calculator, for

$$\sphericalangle A = \frac{\pi}{2} \quad \text{and} \quad \sphericalangle B = \frac{\pi}{6}.$$

2. Express the following as a trigonometric function of a single angle.

$$\sin\left(\frac{\pi}{2}\right) \cos\left(\frac{\pi}{8}\right) - \cos\left(\frac{\pi}{2}\right) \sin\left(\frac{\pi}{8}\right)$$

3. Simplify and then give an exact value for each expression.

a. $\cos 108^\circ \cos 18^\circ + \sin 108^\circ \sin 18^\circ$

b.
$$\frac{\tan\left(\frac{5\pi}{6}\right) - \tan\left(\frac{\pi}{3}\right)}{1 + \tan\left(\frac{5\pi}{6}\right) \tan\left(\frac{\pi}{3}\right)}$$

4. Simplify
- $\cos(x + \pi)$
- .

5. If $\sin A = \frac{2}{7}$ and $\cos B = \frac{3}{5}$, $\sphericalangle A$ is in QII and $\sphericalangle B$ is in QIII, find an exact value for $\cos(A - B)$.

6. Determine the exact value of $\tan\left(\frac{\pi}{12}\right)$.