Name: $\qquad$ Date: $\qquad$

| Learning Goal 4.1 | The Mean Value Theorem and L'Hospital's Rule |
| :--- | :--- |

## Theorem Day!

## The Intermediate Value Theorem

Let $f$ be continuous on $[a, b]$ and let $M$ be any number between $f(a)$ and $f(b)$. Then there exists a number $c$ such that

## Rolle's Theorem

Let $f$ be a function that satisfies the following:

1. $f$ is continuous on $[a, b]$,
2. $f$ is differentiable on $(a, b)$ and
3. $f(a)=f(b)$


## The Mean Value Theorem

Let $f$ be a function that satisfies the following:

1. $f$ is continuous on $[a, b]$,
2. $f$ is differentiable on $(a, b)$ and

Example Show that the equation $x^{3}+x-1=0$ has exactly one root.

Example Determine all the numbers $c$ which satisfies the conclusion of the MVT for $f(x)=x^{3}-x$ on $[0,2]$.

