

Name: \_\_\_\_\_

Date: \_\_\_\_\_

**Learning Goal 8.1**Solving exponential and logarithmic equations with same base and with different bases, including base  $e$ .**Power Law****Product Law****Quotient Law****Example** Evaluate.

a.  $\log_5 75 - \log_5 3$

b.  $\log_2 8$

**Example** Simplify.

a.  $5^{\log_5(a+b)}$

b.  $8^{2 \log_2 m - 1/2 \log_2 n^6}$

**Example** Change of Base

$$\log_b x = \frac{\log_a x}{\log_a b}$$

**Example** Write as a single logarithm.

a.  $\frac{\log_{11} 10}{\log_{11} 5}$

b.  $\frac{\log_3 7}{\log_3 4}$

**Example** Simplify by changing the base of the logarithm. Check using a calculator.

a.  $\log_{27} 9$

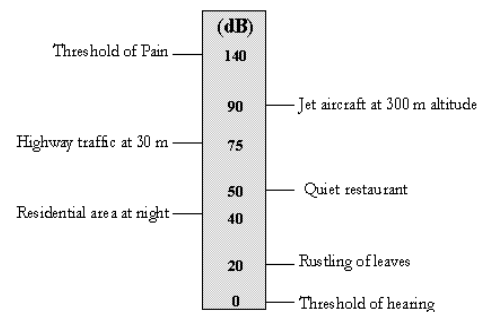
b.  $\log_8 32 + \log_{16} 2$

**Example** Simplify. State any restrictions on the variable.

$$4 \log_3 x - \frac{1}{2} (\log_3 x + 5 \log_3 x)$$

**Example** The decibel scale measures the loudness of sound. Each 10 unit step on the scale represents a 10 fold increase in loudness. The intensity level,  $\beta$  is related to  $I$ , the intensity of the sound, in watts per square metre ( $\text{W}/\text{m}^2$ ) and  $I_0 = 10^{-12} \text{ W}/\text{m}^2$  (the faintest sound that can be heard by a person with normal hearing) by the following:

$$\beta = 10 \log \left( \frac{I}{I_0} \right)$$



Sounds that are at most 100 000 times as intense as a whisper are considered to be safe, no matter how long or how often you hear them. The sound level of a whisper is 20 dB. What sound level can be considered safe, no matter how long it lasts?