

Name: _____

Date: _____

Learning Goal 1.2Factor trinomials of the form $ax^2 + bx + c$.

Expand:

$$\neq x^2 + 25$$

$$\begin{aligned} (x+5)^2 &= (x+5)(x+5) \\ &= x^2 + 5x + 5x + 25 \\ &= x^2 + 10x + 25 \end{aligned}$$

$(x-1)^2 =$

$x^2 - 2x + 1$

$(x-2)^2 =$

$x^2 - 4x + 4$

$(x-3)^2 =$

$x^2 - 6x + 9$

$(x+1)^2 =$

$x^2 + 2x + 1$

$(x+2)^2 =$

$x^2 + 4x + 4$

$(x+3)^2 =$

$x^2 + 6x + 9$

$(2x-1)^2 =$

$4x^2 - 4x + 1$

$(3x-1)^2 =$

$9x^2 - 6x + 1$

$(4x-1)^2 =$

$16x^2 - 8x + 1$

$(2x+1)^2 =$

$4x^2 + 4x + 1$

$(3x+1)^2 =$

$9x^2 + 6x + 1$

$(4x+1)^2 =$

$16x^2 + 8x + 1$

What patterns do you see in the trinomials and their factors above?

$$\begin{aligned} 121x^2 + 22x + 1 \\ = (11x + 1)^2 \end{aligned}$$

$$\begin{aligned} x^2 - 22x + 121 \\ = (x - 11)^2 \end{aligned}$$

How could you use the patterns to factor these trinomials?

$$\begin{array}{l}
 2 \times \sqrt{4 \times 25} \\
 = 2 \times (2 \times 5) \\
 = 2 \times 10 \\
 = \underline{20}
 \end{array}
 \quad
 \begin{array}{l}
 4x^2 + 20x + 25 \\
 = (2x + 5)^2
 \end{array}
 \quad
 \text{and}
 \quad
 \begin{array}{l}
 2 \times \sqrt{9 \times 4} \\
 = 2 \times (3 \times 2) \\
 = 2 \times 6 \\
 = \underline{12}
 \end{array}
 \quad
 \begin{array}{l}
 9x^2 - 12x + 4 \\
 = (3x - 2)^2
 \end{array}$$

This type of polynomial is called a perfect square trinomials.

Example Factor these trinomials

a. $36x^2 + 12x + 1$

$$\begin{array}{l}
 2 \times \sqrt{36 \times 1} = (6x + 1)^2 \\
 = 2 \times (6 \times 1) \\
 = 2 \times 6 \\
 = \underline{12}
 \end{array}$$

b. $16 - 56x + 49x^2$

$$\begin{array}{l}
 2 \times \sqrt{16 \times 49} = (4 - 7x)^2 \\
 = 2 \times (4 \times 7) \\
 = 2 \times 28 \\
 = \underline{56}
 \end{array}$$

How about these?

a. $81m^2 - 49$

$$\begin{array}{l}
 = 81m^2 + 0m - 49 \\
 = (9m + 7)(9m - 7)
 \end{array}$$

Expand:

$$= 81m^2 - 63m + 63m - 49$$

b. $162v^4 - 2w^4$

$$\begin{array}{l}
 = 2(81v^4 - w^4) \\
 = 2(9v^2 + w^2)(9v^2 - w^2)
 \end{array}$$

This type of polynomial is called a difference of squares.