

Name: \_\_\_\_\_

Date: \_\_\_\_\_

**Learning Goal 5.2**

Use exponent laws to evaluate expression with positive and negative rational exponents.

Write each power as a radical, then simplify if possible.

a.  $35^{2/3} = (\sqrt[3]{35})^2$

b.  $32^{3/2} = 2^7\sqrt{2}$

c.  $(-32)^{2/5} = (\sqrt[5]{-32})^2$   
 $= 4$

d.  $400^{1.5} = (\sqrt{400})^3$   
 $= 8000$

e.  $(-125)^{1/3}$   
 $= \sqrt[3]{-125}$   
 $= -5$

f.  $(\frac{8}{125})^{2/3} = (\sqrt[3]{\frac{8}{125}})^2$   
 $= \frac{4}{25}$

g.  $(-1000)^{-2/3}$   
 $= \left(\sqrt[3]{-\frac{1}{1000}}\right)^2$   
 $= \frac{1}{100}$

h.  $(\frac{1}{4})^{-1/2} = \sqrt{4}$   
 $= 2$

i.  $(-0.0008)^{-4/3}$   
 $= \left(\sqrt[3]{-\frac{10000}{8}}\right)^4$   
 $= 1\,600\,000\sqrt[3]{10}$

Write each radical as a fractional power with the smallest possible base.

a.  $\sqrt[3]{81} = 3^{4/3}$

b.  $\sqrt[4]{32} = 2^{5/4}$

c.  $(\sqrt{10})^3 = 10^{3/2}$

d.  $(\sqrt[3]{-10})^2 = (-10)^{2/3}$

e.  $\left(\frac{1}{2\sqrt{2}}\right)^2 = \frac{1}{2^3}$

f.  $(5\sqrt[3]{5})^{-3} = \frac{1}{5^4}$

**Example** Paleontologists use measurements from fossilized dinosaur tracks and the formula

$$v = 0.155s^{5/3}f^{-7/6}$$

to estimate the speed at which the dinosaur travelled. In the formula,  $v$  is the speed in metres per second,  $s$  is the distance between successive footprints of the same foot, and  $f$  is the foot length in metres. If  $s = 1.5$  m and  $f = 0.3$  m, find the estimate the speed of the dinosaur.

$$1.24 \text{ m/s}$$