

$a = 1$

Name: _____

Date: _____

Learning Goal 3.3

Convert standard form of the quadratic equation to vertex form by completing the square.

Convert the following functions into vertex form of the equation.

a. $f(x) = x^2 - 9x - 38$

b. $g(x) = x^2 - 2x + 3$

 $x^2 - 9x + \underline{\hspace{2cm}}$ is a perfect square trinomial? $x^2 - 2x + \underline{\hspace{2cm}}$ is a perfect square trinomial?

$$x^2 - 9x + \frac{81}{4}$$

$$x^2 - 2x + 1$$

$$\begin{aligned} f(x) &= \left(x^2 - 9x + \frac{81}{4}\right) - \frac{81}{4} - 38 \\ &= \left(x^2 - 9x + \frac{81}{4}\right) - \frac{81}{4} - \frac{152}{4} \\ &= \left(x^2 - 9x + \frac{81}{4}\right) - \frac{233}{4} \\ &= \left(x - \frac{9}{2}\right)^2 - \frac{233}{4} \end{aligned}$$

$$\begin{aligned} g(x) &= (x^2 - 2x + 1) - 1 + 3 \\ &= (x^2 - 2x + 1) + 2 \\ &= (x - 1)^2 + 2 \end{aligned}$$

c. $h(x) = x^2 + 10x + 14$

a. $y = x^2 + 16x - 22$

 $x^2 + 10x + \underline{\hspace{2cm}}$ is a perfect square trinomial?
 $x^2 + 10x + 25$ $x^2 + 16x + \underline{\hspace{2cm}}$ is a perfect square trinomial?
 $x^2 + 16x + 64$

$$\begin{aligned} h(x) &= (x^2 + 10x + 25) - 25 + 14 \\ &= (x^2 + 10x + 25) - 11 \\ &= (x + 5)^2 - 11 \end{aligned}$$

$$\begin{aligned} y &= (x^2 + 16x + 64) - 64 - 22 \\ &= (x^2 + 16x + 64) - 86 \\ &= (x + 8)^2 - 86 \end{aligned}$$