

Name: _____

Date: _____

Learning Goal 9.2	Solving quadratic inequalities.
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Example Graph $y < -2(x - 3)^2 + 1$ and determine whether the point $(2, -4)$ is a solution to the inequality.

Recall vertex form:

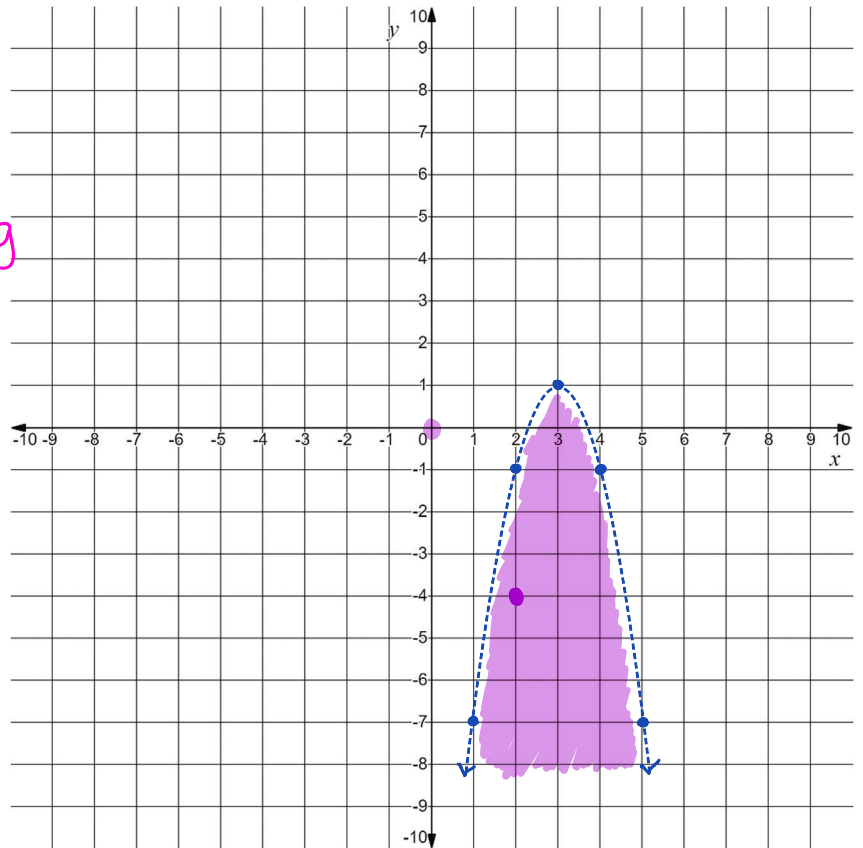
$$y = a(x - p)^2 + q$$

smiling/frowning
vertex @ (p, q)

expansion/
compression

- so our vertex is at $(3, 1)$

- it is frowning with a vertical compression/horizontal expansion of 2.



either a table of values or a 'pseudo' table of values with an exp/comp of 2:

	x	y	
	1	-7	}
	2	-1	
vertex in the middle →	3	1	}
	4	-1	
	5	-7	

mirror

left/right | down

1	$2 \times (1)^2 = 2$
2	$2 \times (2)^2 = 8$
3	$2 \times (3)^2 = 18$

Now for the inequality:
TP: $(0, 0)$ or

$$y < -2(x - 3)^2 + 1$$

$$0 < -2(0 - 3)^2 + 1$$

$$0 < -2(-3)^2 + 1$$

$$0 < -2(9) + 1$$

so $(2, -4)$ is a solution to the inequality

$$(2, -4) \quad y < -2(x - 3)^2 + 1$$

$$-4 < -2(2 - 3)^2 + 1$$

$$-4 < -2(-1)^2 + 1$$

$$-4 < -2 + 1$$

$$-4 < -1 \quad \checkmark$$

$$0 < -18 + 1$$

$$0 < -17$$

Example Graph $y \geq x^2 - 4x - 5$.

Standard form is not
great to graph from.
so

complete the square!

$$y \geq (x^2 - 4x) - 5$$

$$\left(-\frac{4}{2}\right)^2 = (-2)^2 = 4$$

$$y \geq (x^2 - 4x + 4 - 4) - 5$$

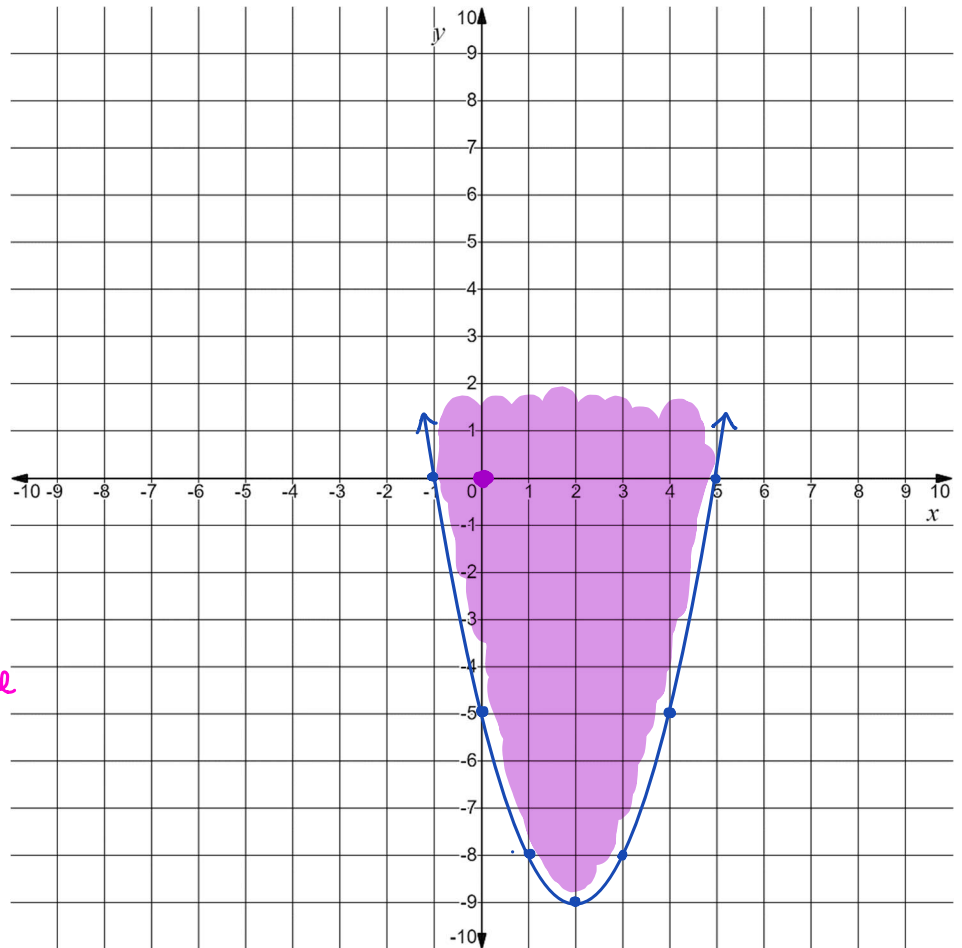
$$y \geq \underbrace{(x^2 - 4x + 4)}_{\text{factor}} - 4 - 5$$

$$y \geq (x - 2)^2 - 9$$

vertex $(2, -9)$

-smiling

-no exp/comp factor



TP: $(0, 0)$ $y \geq x^2 - 4x - 5$.

$$0 \geq (0)^2 - 4(0) - 5$$

$$0 \geq 0 - 0 - 5$$

$$0 \geq -5$$

