

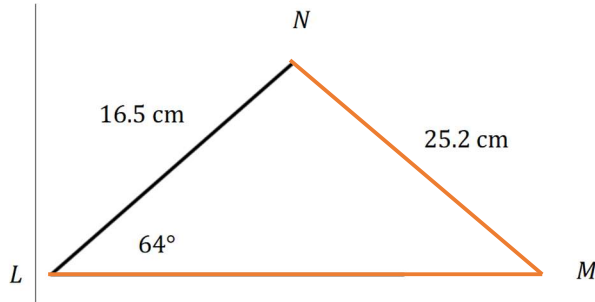
Name: \_\_\_\_\_

Date: \_\_\_\_\_

**Learning Goal 2.3**

Use of sine and cosine laws to solve non-right triangles, including ambiguous cases.

1. In  $\triangle LMN$ ,  $\angle L = 64^\circ$ ,  $l = 25.2$  cm and  $m = 16.5$  cm. Determine the measure of  $\angle N$  to the nearest degree.



Because  $l > m$  and  $\angle L$  is an acute angle, there is only one possible triangle.

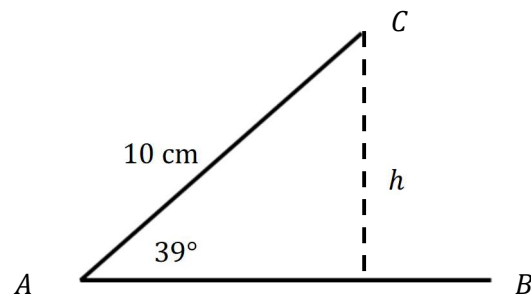
$$\begin{aligned}\frac{\sin L}{l} &= \frac{\sin M}{m} \\ \frac{\sin 64^\circ}{25.2} &= \frac{\sin M}{16.5} \\ 16.5 \times \frac{\sin 64^\circ}{25.2} &= \sin M \\ \angle M &= \sin^{-1}\left(16.5 \times \frac{\sin 64^\circ}{25.2}\right) \\ \angle M &= 37^\circ\end{aligned}$$

$$\begin{aligned}\angle N &= 180^\circ - 64^\circ - 37^\circ \\ \angle N &= 79^\circ\end{aligned}$$

2. In  $\triangle ABC$ ,  $\angle A = 39^\circ$ ,  $a = 6$  cm and  $b = 10$  m. Solve the triangle, leaving all answers to the nearest unit.

Because  $a < b$ , we need to check the height of the triangle first to make sure that the given dimensions **can** create a triangle.

$$\begin{aligned}\sin A &= \frac{h}{b} \\ \sin 39^\circ &= \frac{h}{10} \\ h &= 10 \times \sin 39^\circ \\ h &\approx 6.3 \text{ cm}\end{aligned}$$



So  $a < h$  and therefore there are no solutions.