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## Chapter 4 Review Answers

For each type of question, the achievement level is indicated. Showing work is an important strategy in communicating your knowledge and ideas so please be thorough.

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Learning Goal 4.1 Identify and order irrational numbers.
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- Tell whether each number is rational or irrational.
- For those that are irrational, estimate the value of the radical to one decimal place, without a calculator.
- For those that are rational, evaluate the radical without a calculator. You may use your sheet of perfect numbers (from Section 4.1)

| Developing | Proficient |  |
| :---: | :---: | :---: |
| 1. $\sqrt{81}$ <br> - rational <br> - $=9$ | 2. $\sqrt[5]{100}$ <br> - irrational <br> - $\approx 2.5$ | 3. $\sqrt[4]{2000}$ <br> irrational $\approx 6.7$ |
| 4. $\sqrt{169}$ <br> - rational <br> - $=13$ | 5. $\sqrt[3]{64}$ <br> - rational <br> - $=4$ | 6. $\sqrt[3]{1738}$ <br> - irrational <br> - $\approx 12.0$ |
| 7. $\sqrt{150}$ <br> irrational <br> $\approx 12.2$ | 8. $\sqrt[4]{16}$ <br> - rational <br> - $=2$ | 9. $\sqrt[5]{1864}$ <br> irrational $\approx 4.5$ |
| 10. $\sqrt{125}$ <br> - irrational <br> - $\approx 11.2$ | 11. $\sqrt[3]{81}$ <br> - irrational <br> - $\approx 4.3$ | 12. $\sqrt[3]{100}$ <br> - irrational <br> - $\approx 4.6$ |
| 13. $\sqrt{121}$ <br> - rational <br> - = 11 | 14. $\sqrt[3]{216}$ <br> - rational <br> - $=6$ | 15. $\sqrt[4]{1296}$ <br> - rational <br> - $=6$ |
| 16. $\sqrt{49}$ <br> - rational <br> - $=7$ | 17. $\sqrt[4]{75}$ <br> - irrational <br> - $\approx 2.9$ | 18. $\sqrt[7]{128}$ <br> - rational <br> - $=2$ |
| 19. $\sqrt{200}$ <br> - irrational <br> - $\approx 14.1$ | 20. $\sqrt[4]{81}$ <br> - rational <br> - $=3$ | 21. $\sqrt[5]{248832}$ <br> - rational <br> - $=12$ |

## Developing

| State the index and the radicand of each radical. |  |  |  |
| :---: | :--- | :--- | :--- |
| 1. $\sqrt[3]{64}$ | 3,64 | 2. $\sqrt[4]{20000}$ |  |
| $3 . \sqrt[4]{16}$ | 4,16 | 4. $\sqrt{1738}$ | 4,20000 |

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## Chapter 4 Review Answers

| 5. $\sqrt[3]{216}$ | $6 . \sqrt[5]{1864}$ |  |  |
| :---: | :---: | :---: | :---: |
| 7. $\sqrt[4]{81}$ | 3,216 | 8. $\sqrt[3]{10000}$ | 3,1864 |

## Proficient/Extending

Use a number line to order these numbers from least to greatest, without a calculator.

1. $\sqrt{25}, \sqrt[3]{30} \sqrt[3]{-8}, \sqrt[4]{20}, \sqrt{\frac{144}{9}}$

$$
\sqrt[3]{-8}, \sqrt[4]{20}, \sqrt[3]{30}, \sqrt{\frac{144}{9}}, \sqrt{25}
$$

2. $\sqrt[5]{-243}, \sqrt{4}, \sqrt[3]{\frac{27}{216}}, \sqrt{12}, \sqrt[3]{6}$

$$
\sqrt[5]{-243}, \sqrt[3]{\frac{27}{216}}, \sqrt[3]{6}, \sqrt{4}, \sqrt{12}
$$

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## Chapter 4 Review Answers

For each type of question, the achievement level is indicated. Showing work is an important strategy in communicating your knowledge and ideas so please be thorough.

## Learning Goal 4.2 $\quad$ Express an entire radical as a simplified mixed radical and vice versa.

| Developing | Proficient | Extending |
| :---: | :---: | :---: |
| Write each radical in simplest form, without a calculator. |  |  |
| 1. $\sqrt{125}$ $5 \sqrt{5}$ | 2. $\sqrt[3]{216}$ <br> 6 | 3. $\sqrt{216 k^{3}}$ $6 k \sqrt{6 k}$ |
| 4. $\sqrt{512}$ $2^{4} \sqrt{2}=16 \sqrt{2}$ | 5. $\sqrt[4]{405}$ $3 \sqrt[4]{5}$ | 6. $\begin{array}{r}\sqrt[3]{-96 x y^{4}} \\ 2 y \sqrt[3]{-12 x y}\end{array}$ |
| 7. $\sqrt{80}$ $4 \sqrt{5}$ | 8. $\sqrt[3]{-100}$ $\sqrt[3]{-100}$ | 9. $\sqrt[4]{48 m^{5} n^{4}}$ $2 m n \sqrt[4]{3 m}$ |
| 10. $\sqrt{147}$ $7 \sqrt{3}$ | 11. $\sqrt[3]{80}$ $2 \sqrt[3]{10}$ | $\begin{aligned} & \text { 12. } \sqrt[5]{a^{7} b^{10} c^{2} d^{12}} \\ & \qquad a b^{2} d^{2} \sqrt[5]{a^{2} c^{2} d^{2}} \end{aligned}$ |


| Developing | Proficient | Extending |
| :---: | :---: | :---: |
| Write each mixed radical as an entire radical, without a calculator. |  |  |
| 1. $2 \sqrt{3}$ $\sqrt{2^{2} \times 3}=\sqrt{12}$ | 2. $-2 \sqrt[3]{8}$ $\sqrt[3]{-2^{3} \times 8}=\sqrt[3]{-64}$ | 3. $12 \sqrt{k^{3}}$ $\sqrt{12^{2} k^{3}}=\sqrt{144 k^{3}}$ |
| 4. $3 \sqrt{5}$ $\sqrt{3^{2} \times 5}=\sqrt{45}$ | 5. $5 \sqrt[4]{2}$ $\sqrt[4]{2 \times 5^{4}}=\sqrt[4]{1250}$ | 6. $-x y \sqrt[3]{9 x y^{4}}$ $\sqrt[3]{(-x y)^{3} \times 9 x y^{4}}=\sqrt[3]{-9 x^{4} y^{7}}$ |
| 7. $6 \sqrt{3}$ $\sqrt{3 \times 6^{2}}=\sqrt{108}$ | 8. $6 \sqrt[3]{10}$ $\sqrt[3]{6^{3} \times 10}=\sqrt[3]{2160}$ | 9. $-3 m \sqrt[4]{4 m n^{4}}$ <br> $\sqrt[4]{(-3 m)^{2} \times 4 m n^{4}}=\sqrt[4]{36 m^{3} n^{4}}$ |
| 10. $4 \sqrt{2}$ $\sqrt{2 \times 4^{2}}=\sqrt{32}$ | $\begin{aligned} & \text { 11. }-8 \sqrt[3]{8} \\ & \sqrt[3]{8 \times-8^{3}}=\sqrt[3]{-4096} \end{aligned}$ | $\begin{aligned} & \text { 12. } a^{2} d^{3} \sqrt[5]{a^{3} b^{5} c^{2}} \\ & \sqrt[5]{\left(a^{2} d^{3}\right)^{5} \times a^{3} b^{5} c^{2}} \\ & \quad=\sqrt[5]{a^{13} b^{5} c^{2} d^{15}} \end{aligned}$ |

## Extending

Simplify the radical.

$$
\begin{gathered}
\sqrt[n]{3 \times 2^{n} \times x^{2 n} y^{n+3}} \\
2 x^{2} y^{n} \sqrt[n]{3 y^{3}}
\end{gathered}
$$

Write the mixed radical as an entire radical.

$$
\begin{gathered}
2 a b^{2} \times \sqrt[n]{5 a b^{2}} \\
\sqrt[n]{\left(2 a b^{2}\right)^{n} \times 5 a b^{2}}=\sqrt[n]{2^{n} \times 5 \times a^{n+1} b^{2 n+2}}
\end{gathered}
$$

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Chapter 4 Review Answers
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## Chapter 4 Review Answers

For each type of question, the achievement level is indicated. Showing work is an important strategy in communicating your knowledge and ideas so please be thorough.

| Learning Goal 4.3 | Evaluate expressions with fractional and negative exponents. <br> Connect fractional exponents to radicals, and negative <br> exponents to reciprocals. |
| :--- | :--- |

## Developing

Simplify each power, to a mixed radical where appropriate, without a calculator.

| 1. $20^{1 / 2}$ | 2. $12^{1 / 2}$ | 3. $15^{1 / 3}$ |
| :---: | :---: | :---: |
| $2 \sqrt{5}$ | $2 \sqrt{3}$ | $\sqrt[3]{15}$ |
| 4. $18^{1 / 3}$ $\sqrt[3]{18}$ | 5. $32^{\frac{1}{2}}$ ( $4 \sqrt{2}$ | 6. $\begin{aligned} & \left(\frac{2}{3}\right)^{-4} \\ & \frac{81}{16} \end{aligned}$ |
| 7. $\left(\frac{1}{10}\right)^{-2}$ $100$ | $\left(\frac{5}{2}\right)^{-3}$ <br> 8. $\frac{8}{125}$ | $\left(\frac{6}{2}\right)^{-4}$ <br> 9. $\frac{1}{81}$ |
| Proficient |  |  |
| $\begin{aligned} & \text { 10. } 18^{2 / 3} \\ & 3 \sqrt[3]{2^{2} \times 3}=3 \sqrt[3]{12} \end{aligned}$ | $\begin{aligned} & 11.32^{4 / 3} \\ & 2^{6 \sqrt[3]{2^{2}}}=64 \sqrt[3]{4} \end{aligned}$ | $\begin{aligned} & 12.50^{3 / 2} \\ & 2 \times 5^{3} \sqrt{2}=250 \sqrt{2} \end{aligned}$ |
| $\text { 13. } 125^{2 / 3} 5^{2}=25$ | 14. $27^{5 / 3}$ $3^{5}=243$ | $\text { 15. } 0.5^{-2} \quad 2^{2}=4$ |
| 16. $\left(\frac{1}{4}\right)^{-1 / 2}$ | $\text { 17. } \begin{array}{r} (-1000)^{-2 / 3} \\ \frac{1}{100} \end{array}$ | $\text { 18. } \begin{aligned} &(-0.008)^{-4 / 3} \\ & 5^{4}=625 \end{aligned}$ |


| Developing |  |  |
| :---: | :---: | :---: |
| Express each radical as a power. |  |  |
| 1. $\sqrt{17^{3}}$ $17^{3 / 2}$ | 2. $\sqrt[4]{15^{5}}$ $15^{5 / 4}$ | 3. $\sqrt[2]{12^{6}}$ $12^{2}$ |
| Proficient |  |  |
| 4. $\sqrt{\left(4 x^{2}\right)^{3}}$ $8 x^{3}$ | 5. $\sqrt[3]{64 x^{6}}$ $4 x^{2}$ | 6. $\left(\sqrt[4]{81 a^{8}}\right)^{2}$ $9 a^{4}$ |

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## Chapter 4 Review Answers

## Proficient

Simplify each expression without a calculator. Your answers should contain only positive, whole number exponents.

| 1. | $\begin{gathered} 0.5 x^{-2} \\ \frac{1}{2 x^{2}} \end{gathered}$ | 2. | $\begin{gathered} \left(\frac{a^{2}}{9}\right)^{-1 / 2} \\ \frac{3}{a} \end{gathered}$ | 3. | $\begin{gathered} \left(-8 q^{6}\right)^{-2 / 3} \\ \frac{1}{4 q^{4}} \end{gathered}$ | 4. | $\begin{gathered} \left(-0.027 m^{3}\right)^{-4 / 3} \\ \frac{10000}{81 m^{4}} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Extending |  |  |  |  |  |  |  |
| 5. | $\begin{gathered} \left(12 x^{3} y^{2}\right)^{1 / 2} \\ 2 x y \sqrt{3 x} \end{gathered}$ | 6. | $\begin{aligned} & \left(18 a^{2} b^{5}\right)^{2 / 3} \\ & 3 a b^{3} \sqrt[3]{12 a b} \end{aligned}$ | 7. | $\begin{aligned} & \left(32 m^{2} n^{8}\right)^{3 / 4} \\ & 8 m n^{6} \sqrt[4]{8 m^{2}} \end{aligned}$ | 8. |  |
| 9. | $\frac{\left(64 p^{5} q^{9}\right)^{4 / 3}}{2^{8} p^{6} q^{12} \sqrt[3]{p^{2}}}$ |  | $\begin{gathered} 3 x y\left(\frac{x^{2}}{y^{2}}\right)^{-1 / 2} \\ 3 y^{2} \end{gathered}$ | 11 | $\begin{gathered} \frac{\left(9 a^{3} b^{6}\right)^{-1 / 2}}{\left(3 a^{3} b^{6}\right)^{-2}} \\ 3 a^{4} b^{9} \sqrt{a} \end{gathered}$ |  | $\begin{gathered} \left(8 x^{n+2} y^{n+1}\right)^{2 / n} \\ x^{2} y^{2} \sqrt[n]{2^{6} x^{4} y^{2}} \end{gathered}$ |


| Proficient | Extending |
| :---: | :---: |
| Write each power as a radical in two different ways. | Write each power as a radical in two different ways, then write in simplest form without a calculator. |
| 1. $26^{2 / 5}$ $\sqrt[5]{26^{2}}=(\sqrt[5]{26})^{2}$ | 2. $20^{2 / 3}$ $\sqrt[3]{20^{2}}=(\sqrt[3]{20})^{2}=2 \sqrt[3]{50}$ |
| 3. $19^{3 / 4}$ $\sqrt[4]{19^{3}}=(\sqrt[4]{19})^{3}$ | 4. $25^{2 / 3}$ $\sqrt[3]{25^{2}}=(\sqrt[3]{25})^{2}=5 \sqrt[3]{5}$ |
| 5. $6^{5 / 2}$ $\sqrt{6^{5}}=(\sqrt{6})^{5}$ | 6. $\left(9 n^{4}\right)^{3 / 2}$ $\sqrt{\left(9 n^{4}\right)^{3}}=\left(\sqrt{9 n^{4}}\right)^{3}=27 n^{6}$ |
| 7. $40^{2 / 3}$ $\sqrt[3]{40^{2}}=(\sqrt[3]{40})^{2}$ | 8. $\left(40 a^{3} b^{4}\right)^{2 / 3}$ $\sqrt[3]{\left(40 a^{3} b^{4}\right)^{2}}=\left(\sqrt[3]{40 a^{3} b^{4}}\right)^{2}=4 a^{2} b^{2} \sqrt[3]{25 b^{2}}$ |
| 9. $3^{5 / 4}$ $\sqrt[4]{3^{5}}=(\sqrt[4]{3})^{5}$ | 10. $\left(72 p^{3} q\right)^{5 / 2}$ $\sqrt{\left(72 p^{3} q\right)^{5}}=\left(\sqrt{72 p^{3} q}\right)^{5}=2^{7} 3^{5} p^{7} q^{2} \sqrt{2 p q}$ |

## Extending

Arrange these numbers in order from least to greatest, without using a calculator.

$$
\begin{aligned}
& \sqrt[3]{9}, 9^{3 / 2}, 9,(\sqrt[5]{9})^{4}, 9^{1 / 2} \\
& \sqrt[3]{9}, 9^{1 / 2},(\sqrt[5]{9})^{4}, 9,9^{3 / 2}
\end{aligned}
$$

Suppose you want $\$ 5000$ in three years. The interest rate for a savings account is $2.9 \%$ compounded annually. The money, $P$ dollars, you must invest now is given by the formula

$$
P=5000(1.029)^{-3}
$$

How much must you invest now to have $\$ 5000$ in three years?
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## Chapter 4 Review Answers

For each type of question, the achievement level is indicated. Showing work is an important strategy in communicating your knowledge and ideas so please be thorough.

## Learning Goal 4.4 <br> Use exponent laws to simplify expressions with rational exponents.

## Proficient

Extending
Simplify without using a calculator. Your answers should contain only positive, whole number exponents.

| 1. | $\begin{gathered} 2 m^{2} \cdot 2 m^{3} \\ =4 m^{5} \end{gathered}$ | 2. | $\begin{gathered} \left(x^{-2} x^{-3}\right)^{4} \\ =\frac{1}{x^{20}} \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| 3. | $\begin{gathered} m^{4} \cdot 2 m^{-3} \\ \quad=2 m \end{gathered}$ | 4. | $\begin{aligned} & \left(n^{3}\right)^{-1 / 3} \cdot 2 n^{-1} \\ & =\frac{2}{n^{2}} \end{aligned}$ |
| 5. | $\begin{gathered} \frac{a^{3}}{a^{5}} \cdot a^{-2} \\ =\frac{1}{a^{4}} \\ \hline \end{gathered}$ | 6. | $\begin{gathered} x^{2} y^{-4} \cdot(x y)^{2} \\ =\frac{x^{4}}{y^{2}} \end{gathered}$ |
| 7. | $\begin{gathered} 4 n^{4} \cdot 2 n^{-3} \\ =8 n \end{gathered}$ | 8. | $\begin{gathered} \left(2 x^{4} y^{-3}\right)^{-1} \\ =\frac{y^{3}}{2 x^{4}} \end{gathered}$ |
| 9. | $\begin{gathered} \frac{2 x^{4} y^{-4} z^{-3}}{3 x^{2} y^{-3} z^{4}} \\ =\frac{2 x^{2}}{3 y z^{7}} \end{gathered}$ | 10. | $\begin{gathered} \frac{\left(16 a^{2} b^{6}\right)^{-1 / 2}}{2 a b^{3}} \\ =\frac{1}{8 a^{2} b^{6}} \end{gathered}$ |
| 11. | $\begin{gathered} 2 x^{3} y^{-3} \cdot 2 x^{-1} y^{3} \\ =4 x^{2} \end{gathered}$ | 12. | $\begin{aligned} & \left(\frac{x^{2} y}{y^{-2}}\right)^{-2} \\ & =\frac{1}{x^{4} y^{6}} \end{aligned}$ |
| 13. | $\begin{gathered} 2 y^{5 / 2} \cdot 3 y^{-3} \\ =\frac{6 \sqrt{y}}{y} \end{gathered}$ | 14. | $\begin{gathered} b a^{4} \cdot\left(2 b^{6} a^{4}\right)^{-3 / 2} \\ =\frac{\sqrt{2}}{4 a^{2} b^{8}} \end{gathered}$ |
| 15. | $\begin{gathered} 4 v^{3} \cdot v^{-1 / 3} u^{-2} \\ =\frac{4 v^{2} \sqrt[3]{v^{2}}}{u} \end{gathered}$ | 16. | $\begin{gathered} \frac{\left(2 x^{-3} z^{2}\right)^{3}}{x^{3} y^{4} z^{2} \cdot x^{-4} z^{3}} \\ =\frac{8 z}{x^{8} y^{4}} \end{gathered}$ |
| 17. | $\begin{gathered} 4 a^{3} b^{2} \cdot 3 a^{-4} b^{-3} \\ =\frac{12}{a^{4} b^{3}} \end{gathered}$ | 18. | $\begin{gathered} \frac{\left(16 p m^{-1}\right)^{-1 / 4} \cdot 2 m^{-1} p^{3}}{2 p q^{2}} \\ =\frac{p_{\sqrt[4]{m p^{3}}}^{2 m q^{2}}}{} \end{gathered}$ |

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## Chapter 4 Review Answers

| 19. | $\begin{gathered} \frac{2 y^{3} \cdot 3 x y^{3}}{3 x^{2} y^{4}} \\ =\frac{2 y^{2}}{x} \end{gathered}$ | 20. | $\begin{gathered} \left(m \cdot m^{-2} \cdot n^{5 / 3}\right)^{2} \\ =\frac{n^{3} \sqrt[3]{n}}{m^{2}} \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| 21. | $\begin{gathered} 4 r^{-3} \cdot 2 r^{2} \\ =\frac{8}{r} \end{gathered}$ | 22. | $\begin{gathered} \left(\frac{x^{1 / 2} y^{-2}}{x^{2} y^{1 / 2}}\right)^{4} \\ =\frac{1}{x^{6} y^{10}} \end{gathered}$ |
| 23. | $\begin{gathered} \frac{3 m^{-4}}{m^{3}} \\ =\frac{3}{m^{7}} \end{gathered}$ | 24. | $\begin{aligned} & \frac{\left(x^{3} y^{2}\right)^{3 / 2}}{\left(x^{-1} y^{-2 / 3}\right)^{1 / 4}} \\ = & x^{4} y^{3} \sqrt[4]{x^{3}} \sqrt[6]{y} \\ = & x^{4} y^{32} \sqrt{x^{9} y^{2}} \end{aligned}$ |
| 25. | $\begin{gathered} 2 k^{4} \cdot 4 k \\ =8 k^{5} \end{gathered}$ | 26. | $\begin{gathered} \frac{\left(x^{-1 / 2} y^{2}\right)^{-5 / 4}}{x^{2} y^{1 / 2}} \\ =\frac{\sqrt[8]{x^{5}}}{x^{2} y^{3}} \end{gathered}$ |

## Extending

## Write 3 different expressions for each result.

1. $x^{3 / 2}$ as the product of two powers with rational exponents.

$$
x \times x^{1 / 2}=x^{-1} \times x^{5 / 2}=x^{-3 / 2} \times x^{3}
$$

2. $x^{3 / 2}$ as the quotient of two powers with rational exponents.

$$
\frac{x^{2}}{x^{1 / 2}}=\frac{x}{x^{-1 / 2}}=\frac{x^{5 / 2}}{x}
$$

3. $x^{3 / 2}$ as the result of raising a power with a rational exponent to a rational exponent.

$$
\left(x^{1 / 2}\right)^{3}=\left(x^{3}\right)^{1 / 2}=\left(x^{3 / 5}\right)^{5 / 2}
$$

Simplify and write as both a power and a radical.

$$
\begin{array}{c|c|c}
\hline\left(\sqrt[3]{x^{4}}\right)\left(\sqrt[5]{x^{2}}\right) & \left(\sqrt{y^{3}}\right)\left(\sqrt[5]{y^{4}}\right) & \sqrt{\sqrt[3]{a^{5} b^{6}}} \\
x^{26 / 15}=(\sqrt[15]{x})^{26} & x^{23 / 10}=\sqrt[10]{x^{23}} & a^{5 / 6} b=b \sqrt[6]{a^{5}} \\
\hline
\end{array}
$$

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## Chapter 4 Review Answers

## Extending

Scientists use the formula

$$
d=0.099 \mathrm{~m}^{9 / 10}
$$

to calculate the volume of water, $d$ litres, that a mammal with mass $m$ kilograms should drink in one day. Calculate how much water a 550 kg moose should drink in 3 days.

