

Name: \_\_\_\_\_

Date: \_\_\_\_\_

<b>Learning Goal 0.2</b>	Expectations for algebra from previous years.
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exp.

Power Law	Product Law	Quotient Law	Change of Base
$(x^a)^b = x^{a \cdot b}$	$x^a x^b = x^{a+b}$	$\frac{x^a}{x^b} = x^{a-b}$	—
$\log(x^a) = a \log x$	$\log(xy) = \log x + \log y$	$\log\left(\frac{x}{y}\right) = \log x - \log y$	$\log_b x = \frac{\log_a x}{\log_a b}$

$\log(x+y) \neq \log x + \log y$

**Example** Simplify the following expression, stating any possible restrictions on the variable.

a.  $\log_8 32 + \log_{16} 2$  \* SO MANY POWERS OF 2

$$\begin{aligned}
 &= \frac{\log_2 32}{\log_2 8} + \frac{\log_2 2}{\log_2 16} \\
 &= \frac{5}{3} + \frac{1}{4} \\
 &= \frac{20}{12} + \frac{3}{12} = \frac{23}{12}
 \end{aligned}$$

b.  $4 \log_3 x - \frac{1}{2}(\log_3 x + 5 \log_3 x)$  POWER

$$\begin{aligned}
 &= 4 \log_3 x - \frac{1}{2}(\log_3 x + \log_3 x^5) \text{ PRODUCT} \\
 &= 4 \log_3 x - \frac{1}{2} \log_3 x^6 \text{ POWER} \\
 &= \log_3 x^4 - \log_3 (x^6)^{1/2} \\
 &= \log_3 x^4 - \log_3 x^3 \text{ QUOTIENT} \\
 &= \log_3 x
 \end{aligned}$$

c.  $\log_7 x^4 + \frac{1}{3}(\log_7 x^2 - \log_7 \sqrt{5x})$  QUOTIENT

$$\begin{aligned}
 &= \log_7 x^4 + \frac{1}{3}(\log_7 x^2 - \log_7 (5x)^{1/2}) \\
 &= \log_7 x^4 + \frac{1}{3} \log_7 \left(\frac{x^2}{(5x)^{1/2}}\right) \text{ POWER} \\
 &= \log_7 x^4 + \log_7 \left(\frac{x^2}{(5x)^{1/2}}\right)^{1/3} \\
 &= \log_7 x^{4 + \frac{8}{3}} + \log_7 \left(\frac{x^{1/2}}{5^{1/6}}\right) \text{ PRODUCT} \\
 &= \log_7 \left(\frac{x^{9/2}}{5^{1/6}}\right)
 \end{aligned}$$

d.  $\frac{\log 16x^8}{4} - \frac{\log 27x}{3}$  POWER LAW

$$\begin{aligned}
 &= \frac{1}{4} \log(16x^8) - \frac{1}{3} \log(27x) \\
 &= \log(16x^8)^{1/4} - \log(27x)^{1/3} \\
 &= \log(2x^2) - \log(3x^{1/3}) \text{ QUOTIENT} \\
 &= \log\left(\frac{2x^2}{3x^{1/3}}\right) \\
 &= \log\left(\frac{2x^{5/3}}{3}\right) \\
 &= \log\left(\frac{2x \times \sqrt[3]{x^2}}{3}\right)
 \end{aligned}$$

Assignment

Handout

Quiz Next Day!

**Example** Solve for  $x$ . State any restrictions on the variable and verify your answers.

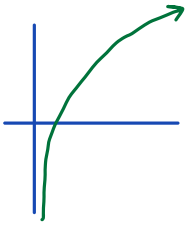
a.  $\log_2 x = \log_2 18 - \log_2 6$  Quotient

$$\log_2 x = \log_2 \left( \frac{18}{6} \right)$$

$$\log_2 x = \log_2 3$$

$$x = 3 \quad \checkmark$$

NPV:  $x > 0$



b.  $64^{3x-1} = \left( \frac{1}{16} \right)^{2x+4}$

$$(2^6)^{3x-1} = (2^{-4})^{2x+4}$$

$$\log(2^{6(3x-1)}) = \log(2^{-4(2x+4)})$$

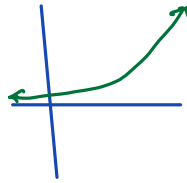
$$6(3x-1) = -4(2x+4)$$

$$18x - 6 = -8x - 16$$

$$18x = -8x - 10$$

$$26x = -10$$

$$x = \frac{-10}{26} = \frac{-5}{13}$$



c.  $2 \log(3-x) = \log 4 + \log(6-x)$  Power

$$\log(3-x)^2 = \log 4 + \log(6-x)$$
 Product

$$\log(3-x)^2 = \log 4(6-x)$$

$$(3-x)^2 = 4(6-x)$$

$$9 - 6x + x^2 = 24 - 4x$$

$$x^2 - 2x - 15 = 0$$

$$(x-5)(x+3) = 0$$

$$x = 5 \quad \text{or} \quad x = -3$$

extraneous.

$$\begin{aligned} 3-x > 0 \\ 3 > x \end{aligned}$$

$$\begin{aligned} 6-x > 0 \\ 6 > x \end{aligned}$$



d.  $\log(4^{2x-3}) = \log(3^{x+2})$  Power

$$\log(4^{2x-3}) = \log(3^{x+2})$$

$$(2x-3)\log 4 = (x+2)\log 3$$

$$(2\log 4)x - 3\log 4 = (\log 3)x + 2\log 3$$

$$(\log 16)x - \log 64 = (\log 3)x + \log 9$$

$$(\log 16)x - (\log 3)x - \log 64 = \log 9$$

$$x(\log 16 - \log 3) = \log 9 + \log 64$$

$$x = \frac{\log 9 + \log 64}{\log 16 - \log 3}$$