

Name: \_\_\_\_\_

Date: \_\_\_\_\_

Equation of a Line	
Slope-Intercept Form $y = mx + b$ <i>y-int.</i> ↑ slope	Slope-Point Form $y - y_1 = m(x - x_1)$ goes through $(x_1, y_1)$
General Form $ax + by + c = 0$ $a \in \mathbb{N}$ , $b, c \in \mathbb{Z}$	Standard Form $ax + by = c$ $a \in \mathbb{N}$ , $b, c \in \mathbb{Z}$
Slope $\text{slope} = m = \frac{\text{rise}}{\text{run}} = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$	

**Warmup** Classify each equation as being in the form:

- Slope-Intercept,
- General,
- Slope-Point form,
- Standard, or
- If the equation is none of these write "none."

$2x + 7y + 9 = 0$ <i>General</i>	$y - 9 = \frac{4}{5}(x + 2)$ <i>slope-point</i>	$3x + \frac{8}{7}y - 10 = 0$ <i>none</i>
$x + 9 = y$ <i>slope-intercept</i>	$(y + 3) = 5(x - 7)$ <i>slope-point</i>	$y = -\frac{4}{5}x^3 - 9$ <i>none</i>
$y = -\frac{8}{9}x + 13$ <i>slope-intercept</i>	$-4y + 3x = 9$ <i>none</i>	$x + 15 = \frac{3}{4}(y - 9)$ <i>none</i>

**Example** Find the equation of a line with slope  $-\frac{7}{9}$  and y-intercept of 12.

$$y = -\frac{7}{9}x + 12$$

Slope-intercept

$$y = mx + b$$

**Example** Find the equation of a line with a slope of  $\frac{3}{5}$  through the point  $(2, 8)$ .

$$y - 8 = \frac{3}{5}(x - 2)$$

slope-point

$$y - y_1 = m(x - x_1)$$

**Example** Find the equation of a line through  $(5, -20)$  and  $(40, 50)$ .

$$\begin{aligned} m &= \frac{50 - (-20)}{40 - 5} \\ &= \frac{70}{35} = 2 \end{aligned}$$

$$\textcircled{1} \quad y + 20 = 2(x - 5)$$

slope-point

$$y - y_1 = m(x - x_1)$$

$$\textcircled{2} \quad y - 50 = 2(x - 40)$$

**Example** A line has a slope of  $-5$  and a x-intercept of  $\frac{5}{2}$ . Find the equation of the line. Write your final equation in slope-intercept form.

$$y - 0 = -5(x - \frac{5}{2})$$

$$(\frac{5}{2}, 0)$$

slope-point

$$y - y_1 = m(x - x_1)$$

$$y = -5(x - \frac{5}{2})$$

$$y = -5x + \frac{25}{2}$$

slope-intercept

**Example** A line has the same slope as the line  $2x + 9y - 39 = 0$  and the same y-intercept as

$$y - 8 = \frac{3}{4}(x - 16)$$

① Slope.

$$(\frac{39}{2}, 0) \quad x\text{-int } (y=0)$$

$$(0, \frac{39}{9}) \quad y\text{-int } (x=0)$$

$$\begin{aligned} m &= \frac{\frac{39}{9} - 0}{0 - \frac{39}{2}} = \frac{\frac{39}{9}}{-\frac{39}{2}} = \frac{39}{9} \times -\frac{2}{39} \\ &= -\frac{2}{9} \end{aligned}$$

② y-int ( $x=0$ )

$$y - 8 = \frac{3}{4}(0 - 16)$$

$$y - 8 = \frac{3}{4}(-16)$$

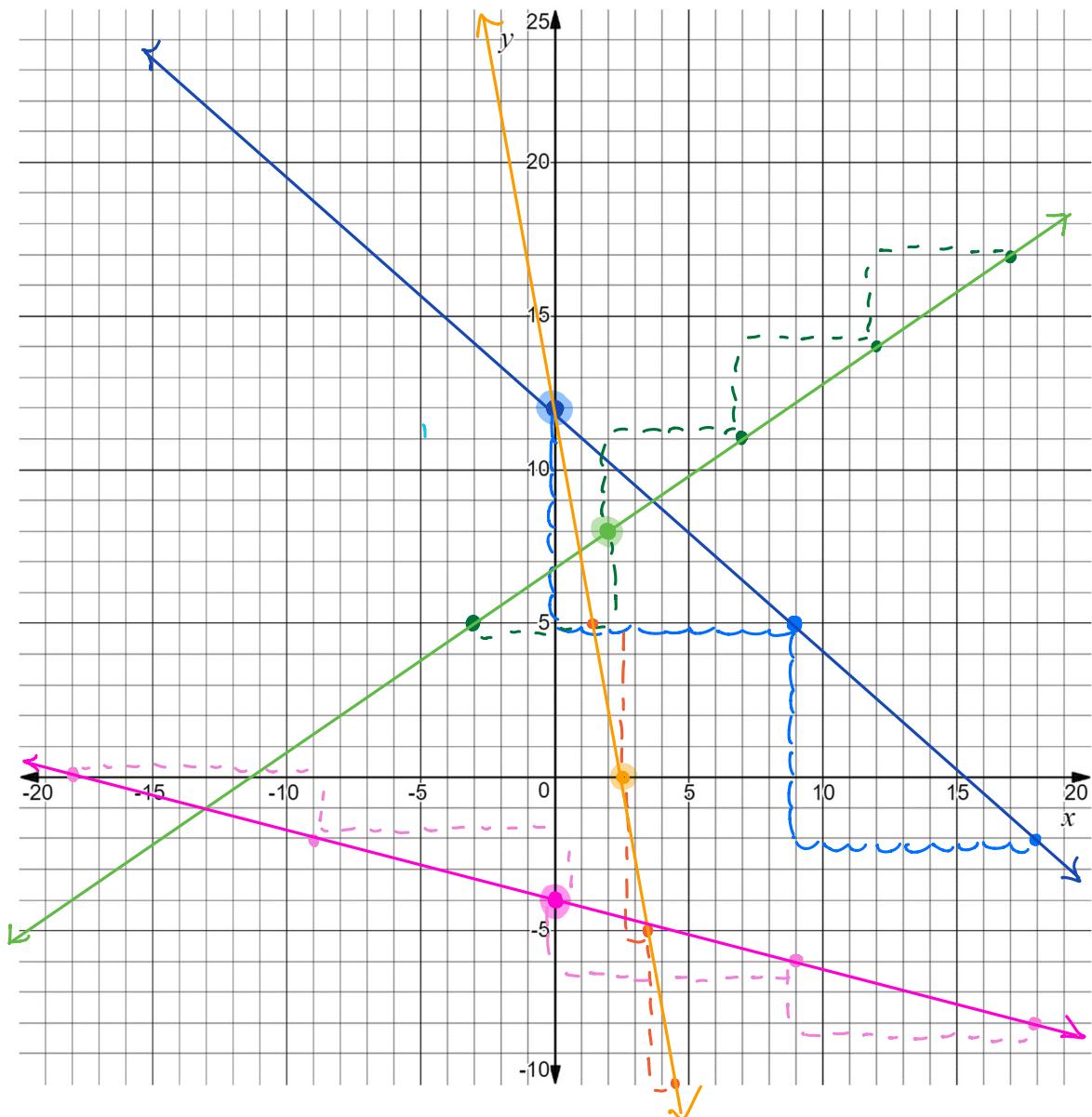
$$y - 8 = -12$$

$$+8 \quad +8$$

$$y = -4$$

③ Equation:  $y = -\frac{2}{9}x - 4$

**Example** Graph all the lines that you found on the previous page.



$$y = -\frac{1}{9}x + 12$$

$$y - 8 = \frac{3}{5}(x - 2)$$

$$y - 0 = -5\left(x - \frac{5}{2}\right)$$

$$y = -\frac{2}{9}x - 4$$