

$$A_{\Delta A} = \frac{b \times h}{2}$$

$$= \frac{\cos z \times \sin z}{2}$$

$$\frac{\pi r^2}{2\pi} = \frac{A_{\square}}{z} \quad r=1$$

$$A_{\square} = \frac{z}{2}$$

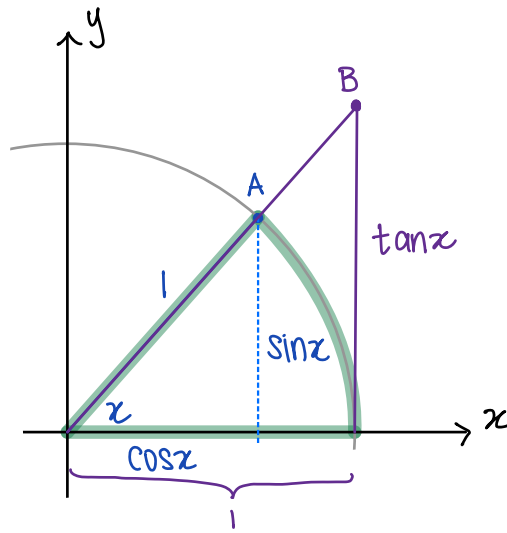
$$A_{\Delta A} \leq A_{\square}$$

$$\frac{\sin z \cos z}{2} \leq \frac{z}{2}$$

$$\frac{\sin z \cos z}{\cos z} \leq \frac{z}{\cos z}$$

$$z \div \sin z \leq \frac{z \div z}{\cos z}$$

$$\boxed{\frac{\sin z}{z} \leq \frac{1}{\cos z}}$$



$$\tan z = \frac{y}{z} \quad z=1$$

$$y = \tan z$$

$$A_{\Delta B} = \frac{b \times h}{2}$$

$$= \frac{1 \times \tan z}{2}$$

$$= \frac{\tan z}{2}$$

$$A_{\Delta B} \geq A_{\square}$$

$$\frac{\tan z}{2} \geq \frac{z}{2}$$

$$\cos z \times \frac{\sin z}{\cos z} \geq z \times \cos z$$

$$\frac{\sin z}{z} \geq \frac{z \cos z}{z}$$

$$\boxed{\frac{\sin z}{z} \geq \cos z}$$

$$\cos z \leq \frac{\sin z}{z} \leq \frac{1}{\cos z}$$

squeeze!

$$\lim_{z \rightarrow 0} \cos z = 1$$

$$\lim_{z \rightarrow 0} \frac{1}{\cos z} = 1$$

$$\Rightarrow \lim_{z \rightarrow 0} \frac{\sin z}{z} = 1$$

and now we can use this as an identity when solving other limits!